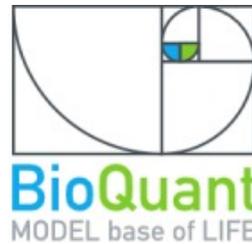


Competition between efficiency and selectivity in ring assembly

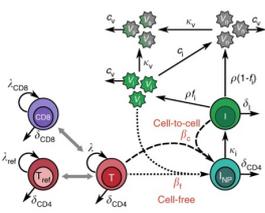
Ulrich Schwarz

Heidelberg University
Institute for Theoretical Physics and BioQuant

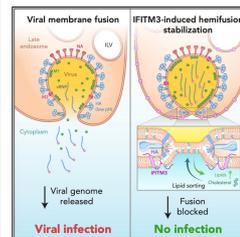


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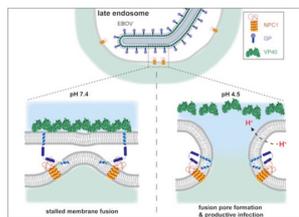
Recent work on viruses



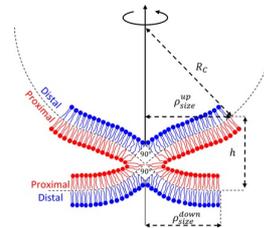
Imle et al.,
Environmental
restrictions
shape HIV-1
spread in 3D
cultures, Nat
Comms 2019



Klein et al., IFITM3
blocks influenza
virus entry by
sorting lipids and
stabilizing
hemifusion, Cell
Host Microbe 2023



Winter et al., The Ebola virus VP40 matrix layer
undergoes endosomal disassembly essential
for membrane fusion, EMBO J 2023



Golani and Schwarz, High curvature promotes
fusion of lipid membranes: Predictions from
continuum elastic theory, Biophys J 2023

2

Recent work on SAS-6 rings



ARTICLE [Check for updates](#)

<https://doi.org/10.1038/s41467-021-26329-1> OPEN

Kinetic and structural roles for the surface in
guiding archite

The Journal of Chemical Physics ARTICLE scitation.org/journal/jcp

Nicolò Banterl
Charlène Brillar
Frauke Gräter

Grand canonical Brownian dynamics simulations of adsorption and self-assembly of SAS-6 rings on a surface

NATURE.COM

Cite as: J. Chem. Phys. 158, 085102 (2023); doi: 10.1063/5.0135349
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Published Online: 23 February 2023

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Santiago Gomez Melo,^{1,2} Dennis Wörthmüller,^{1,2} Pierre Gönczy,³ Niccolo Banterle,^{3,4} and Ulrich S. Schwarz^{1,2,a)}

3

Collaborators on SAS-6 projects

- **SAS-6:** Pierre Gönczy, EPFL; Niccolo Banterle, EMBL Heidelberg; Paul Guichard & Virginie Hamel, Uni Geneva
- **HS-AFM:** Adrian Nievergelt and Georg Fanter, EPFL
- **Molecular dynamics:** Svenja de Buhr and Frauke Gräter, Heidelberg
- **Own students:** Heinrich Klein, Dennis Wörthmüller, Santiago Gomez-Melo

4

SAS-6 rings in 3D

5

Cilia, flagella, centrioles, centrosomes, spindles

PhD thesis TB Warrington

Cilia are cellular appendages that can beat. Our body is full of them. Moreover, most of our cells have a primary cilium. **Flagella** have the same basic structure as motile cilia.

Centrioles organize the microtubules in our cells and have the same basic architecture as cilia. Two centrioles form the **centrosome** and the **spindle poles**.

SAS-6 ring

[P. Gönczy Nature Reviews 2012]

6

9-fold symmetry and the SAS-6 ring

Wikipedia

All cilia, flagella and centrioles have a 9-fold symmetry that results from the self-assembly of the Spindle assembly abnormal protein 6 (SAS-6).

[P. Gönczy Nature Reviews 2012]

7

Relevant dissociation constants and concentrations

$K_d \sim 60 \mu M$

$K_d \sim 1 \mu M$

Cytoplasm
 $\sim 0.1 \mu M$

Centrosome
 $\sim 5 \mu M$

How can SAS-6 form rings ?

[Klein et al. Sci Reports 2016]

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Patchy particles computer simulations

SAS6 assembly

Heinrich C. R. Klein, Paul Guichard, Virginie Hamel
Pierre Gönczy and Ulrich S. Schwarz

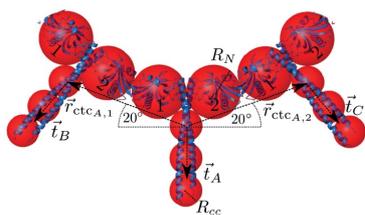
Bulk assembly

with homodimer concentration $75\mu\text{M}$

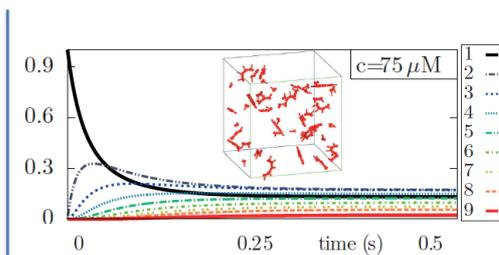
[Klein et al. Sci Reports 2016]

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Simulation setup

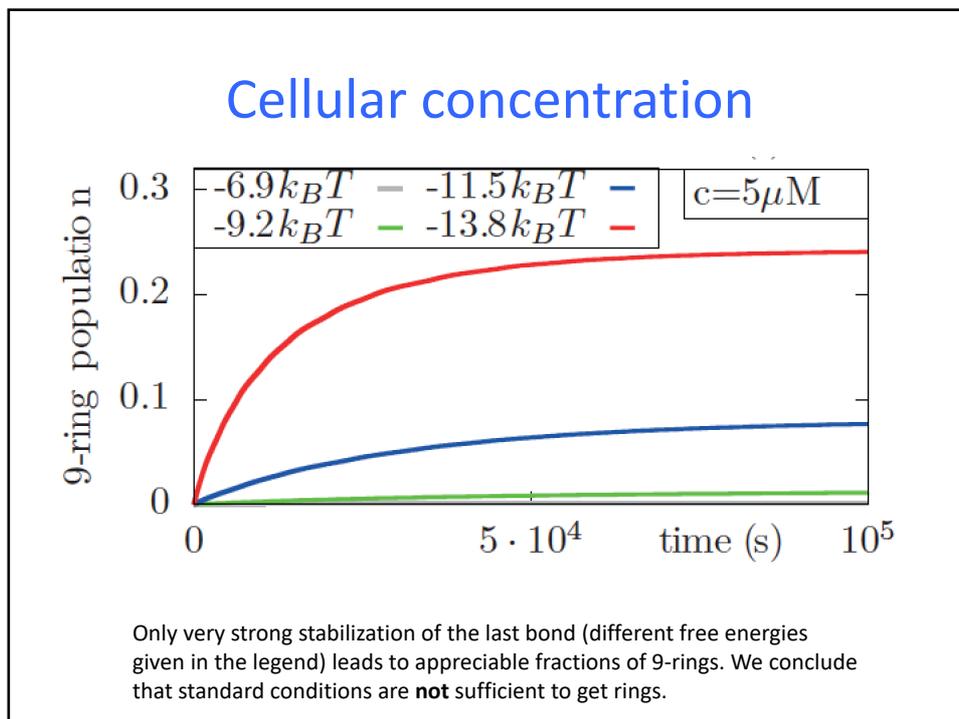


A rigid patchy particle model for the SAS-6 homo-dimers was built from Protein Data Bank (PDB) structures 3Q0X and 3Q0Y.



At $75\mu\text{M}$, well above the centriolar concentration of $5\mu\text{M}$, steady state is reached within seconds, but only small oligomers form, in agreement with *in vitro* experiments.

10



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Patchy particles computer simulations with half-spherical scaffold

SAS6 assembly

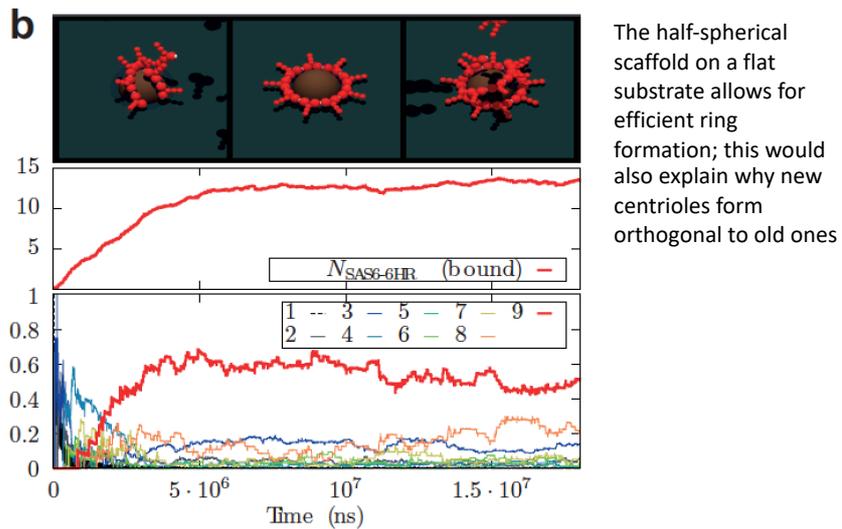
Heinrich C. R. Klein, Paul Guichard, Virginie Hamel
Pierre Gönczy and Ulrich S. Schwarz

Spherical scaffold
embedded in a planar surface
with homodimer concentration $5\mu\text{M}$

[Klein et al. Sci Reports 2016]

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Potential role of a half-spherical scaffolds on a flat substrate

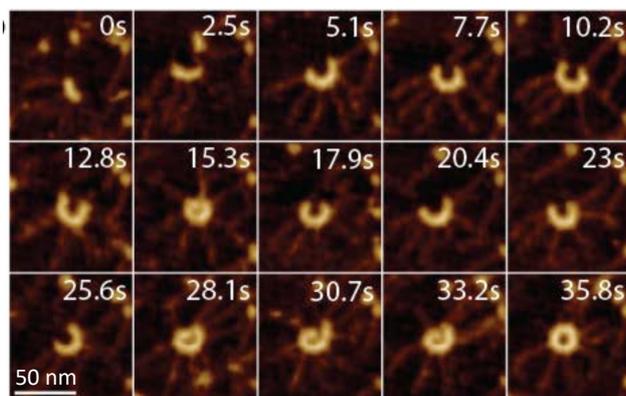


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SAS-6 rings on a surface

15

HS-AFM imaging with photothermal off-resonance tapping (PORT)

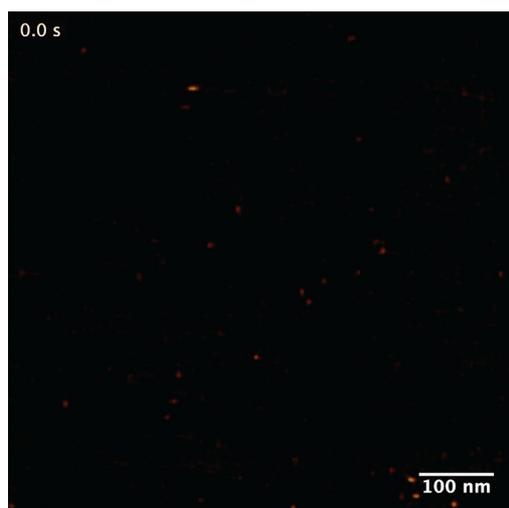


HS-PORT is sufficiently gentle such that SAS-6 ring assembly can be monitored with high temporal and spatial resolution.

[Nievergelt, Banterle et al. Nature Nanotech 2018]

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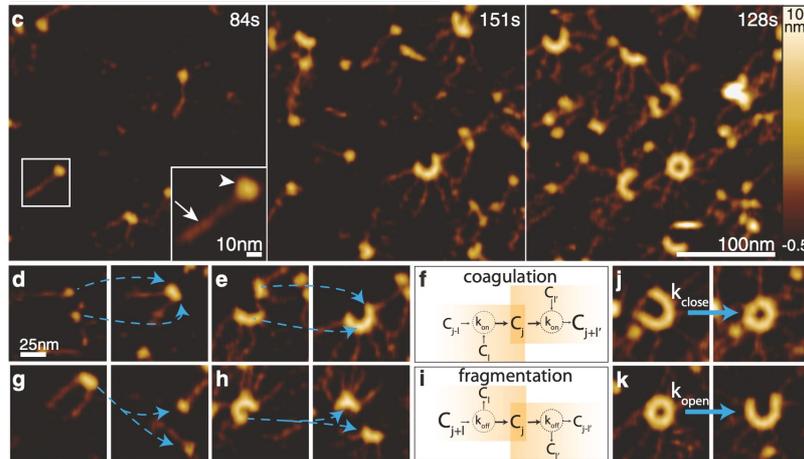
Dynamics of SAS-6 ring assembly



[Banterle et al. Nat Comms 2021]

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Oligomers of different sizes interact

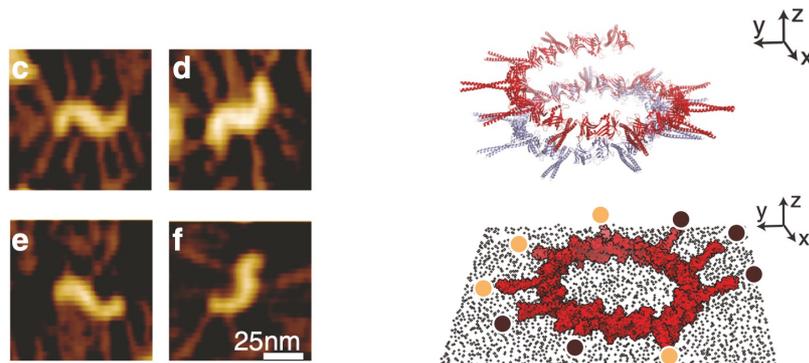


Both coagulation and fragmentation events are observed.

[Banterle et al. Nat Comms 2021]

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Malformed structures



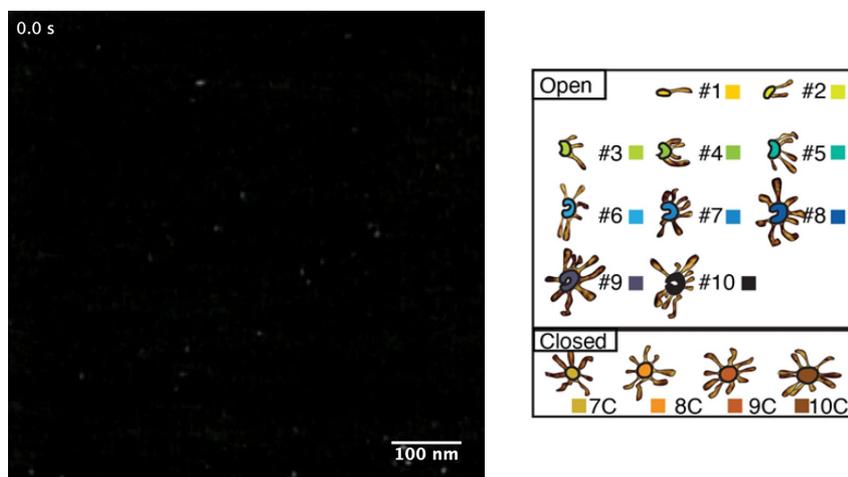
The HS-AFM sometimes shows S-shaped structures that most likely are 3D spirals adsorbed to the 2D surface („squeelices“).

Molecular dynamics (MD) computer simulations confirm that SAS-6 in solution forms spirals that become strained rings on the surface.

[Banterle et al. Nat Comms 2021]

20

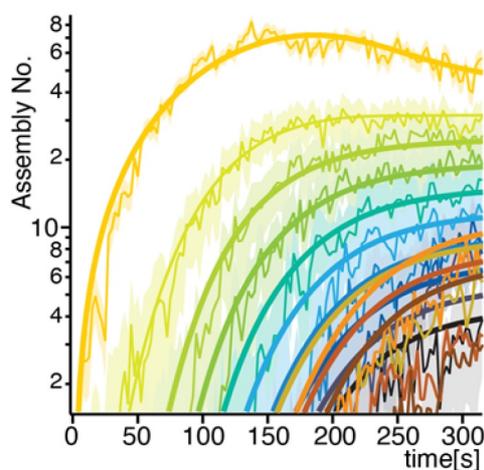
Intermediates can be classified by image processing (ilastik)



[Banterle et al. Nat Comms 2021]

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Quantitative analysis of ring assembly



[Banterle et al. Nat Comms 2021]

- Monomer concentration first increases due to adsorption of SAS-6 homodimers onto mica surface
- Equilibrium not established in these traces, but relaxation towards equilibrium is visible
- Assembly curves can be fitted to coagulation-fragmentation model
- Surface dramatically improves self-assembly for kinetic and structural reasons

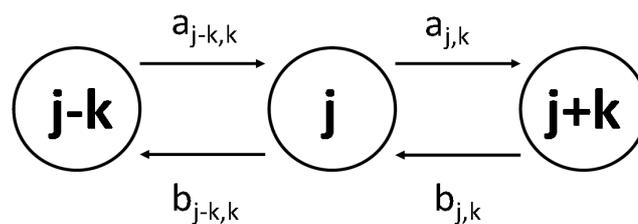
22

Theoretical analysis: coagulation-fragmentation (CF) equations

- Standard approach for reversible assembly of clusters and polymers
- Go back to Smoluchowski 1916, Becker and Döring 1935, Kolmogorov 1941
- Widely used not only in biophysics and soft matter physics, but also in astrophysics, environmental physics, geosciences, etc

23

Reaction scheme for CF-equations



A cluster of size j can either

1. coagulate with a cluster of size k to become a cluster of size $j+k$
2. or fragment into two clusters of sizes $j-k$ and k , respectively

The association and dissociation rates a and b are labeled with the cluster sizes.

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CF-equations for complexes of maximal size N

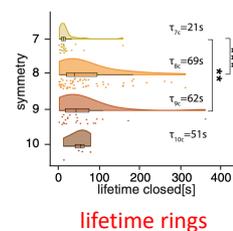
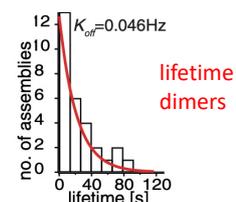
$$\dot{c}_j(t) = \frac{1}{2} \sum_{k=1}^{j-1} a_{j-k,k} c_{j-k} c_k - \sum_{k=1}^{N-j} a_{j,k} c_j c_k - \frac{1}{2} \sum_{k=1}^{j-1} b_{j-k,k} c_j + \sum_{k=1}^{N-j} b_{j,k} c_{j+k}$$

- System of ordinary differential equations for the concentrations $c_j(t)$ of the clusters of size j as a function of time t
- Mass action kinetics; because of the binary coagulation terms, the equations are non-linear
- Gain and loss terms have plus and minus signs, respectively
- The factors $\frac{1}{2}$ avoid overcounting ($1+4 \rightarrow 5$ is the same process as $4+1 \rightarrow 5$)
- In 3D association rates a are measured in $1/Ms$ or m^3/s ; in 2D they are measured in m^2/s ; dissociation rates b are measured in $1/s$
- The CF-equations obey mass conservation: $\sum_{j=1}^N j \dot{c}_j(t) = 0$
- SAS-6 rings: $N=9$; for macroscopic systems, one often uses $N \rightarrow \infty$.

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Fit of CA-model to SAS-6 assembly

- Average lifetime of dimers is 22 s
- Rings of 7-10 are observed; 9-rings have the largest lifetimes; 7-rings exist, but are unstable due to large strain
- Association time is estimate from overall fit to CA-model
- This leads to central result $K_d = 79$ dimers/ μm^2
- Surface concentration $c=500$ dimers/ μm^2
 $\Rightarrow R_{surf}=c/K_d=10$, assembly is possible
- Compare bulk: $c=120$ nM, $K_d=60$ $\mu M \Rightarrow R_{bulk}=c/K_d=10^{-3}$, assembly is not possible
- Surface shifts assembly kinetics by four orders of magnitude in this experiment

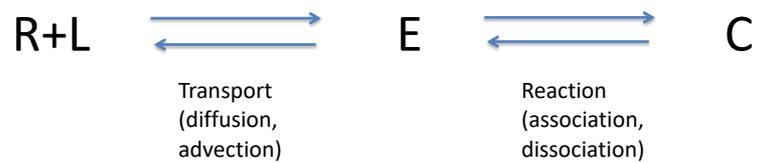


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Reaction versus diffusion limits

31

Protein-protein binding involves diffusion and reaction

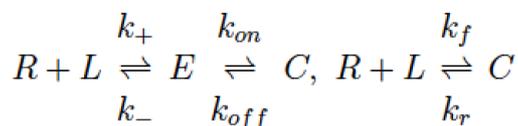


This concept is helpful even when the encounter state is not well-defined.

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Binding as 2-step process

We introduce the encounter complex as intermediate step:



Steady state assumption for E:

$$k_f = \frac{k_+ k_{on}}{k_- + k_{on}}, \quad k_r = \frac{k_- k_{off}}{k_- + k_{on}}$$

$$k_- \ll k_{on} \quad k_f = k_+, \quad k_r = k_- \frac{k_{off}}{k_{on}} \quad \text{diffusion control}$$

$$k_- \gg k_{on} \quad k_f = k_{on} \frac{k_+}{k_-}, \quad k_r = k_{off} \quad \text{reaction control}$$

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Binding as 2-step process - continued

A convenient way to rewrite our results:

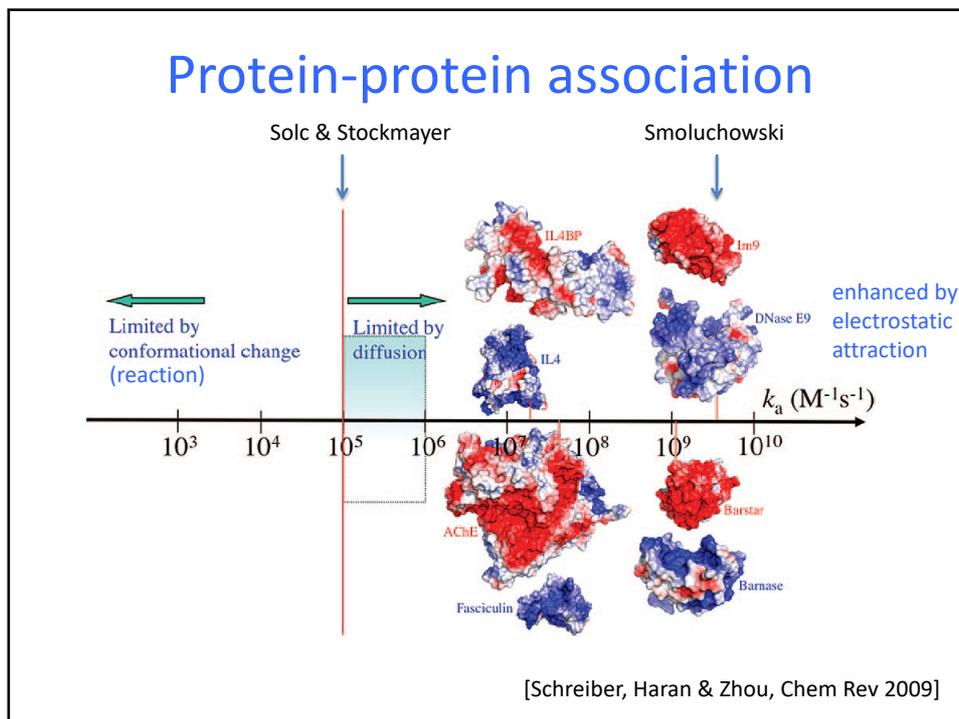
$$\frac{1}{k_f} = \frac{1}{k_+} + \frac{1}{k_{on}} \frac{k_-}{k_+}, \quad \frac{1}{k_r} = \frac{1}{k_-} \frac{k_{on}}{k_{off}} + \frac{1}{k_{off}}$$

Diffusion rates from solving the diffusion equation (Smoluchowski rates):

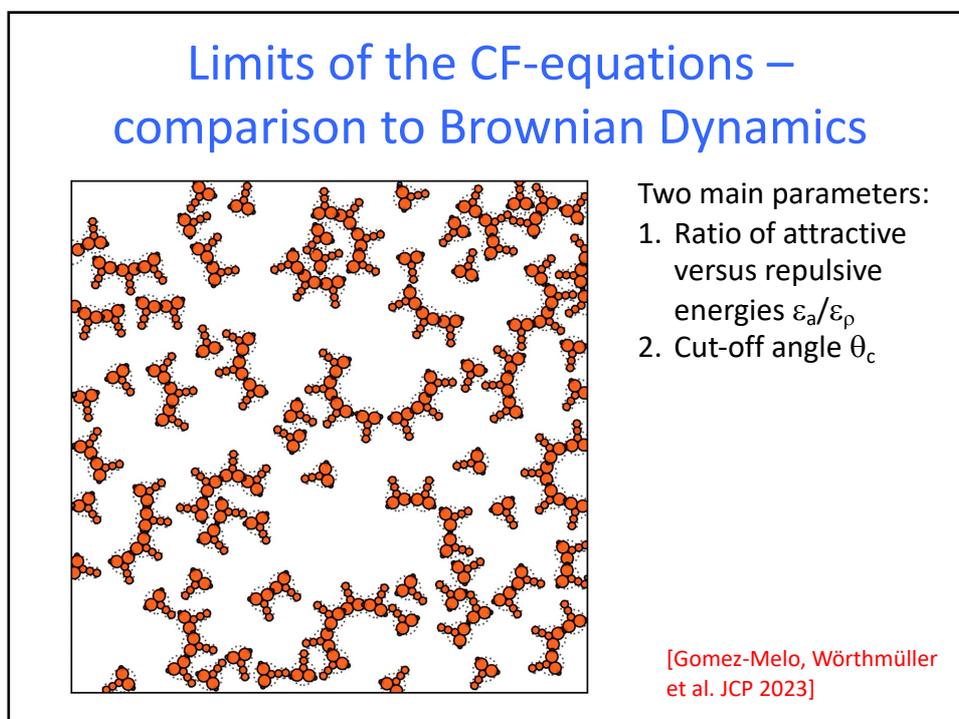
$$k_+ = 4\pi Ds, \quad k_- = \frac{3D}{s^2}$$

The diffusion constant D is universal due to the Stokes-Einstein relation (around $(10 \text{ um})^2/\text{s}$ with $s=4 \text{ nm}$). A typical value for the Smoluchowski association rate therefore is $6 \times 10^9 \text{ 1/Ms}$. This is reduced by 4-5 orders of magnitude if one considers orientational degrees of freedom (Solc and Stockmayer).

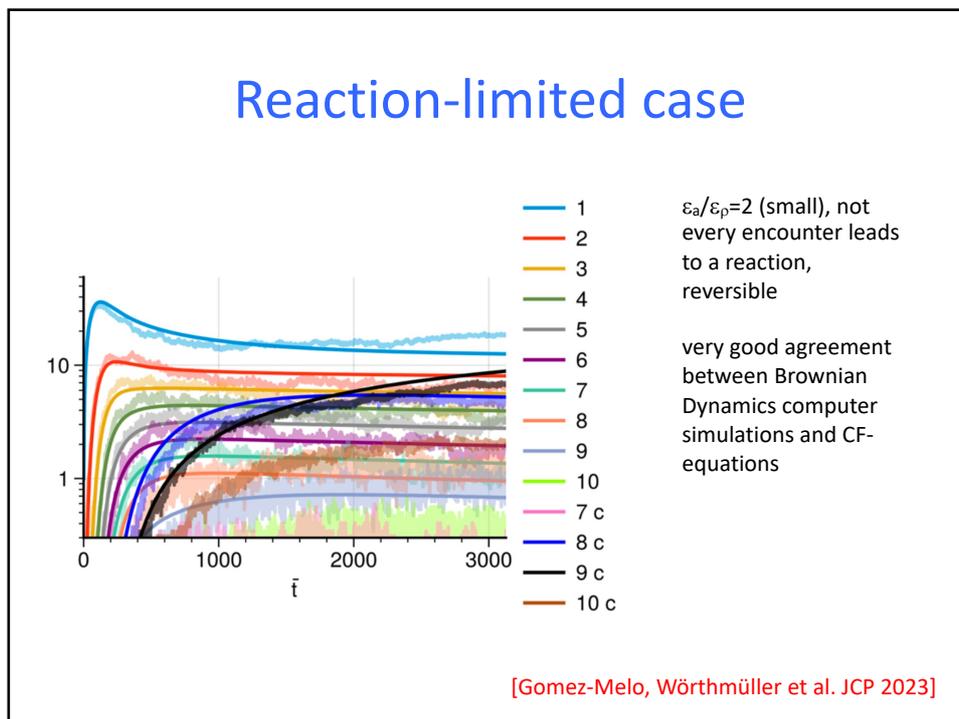
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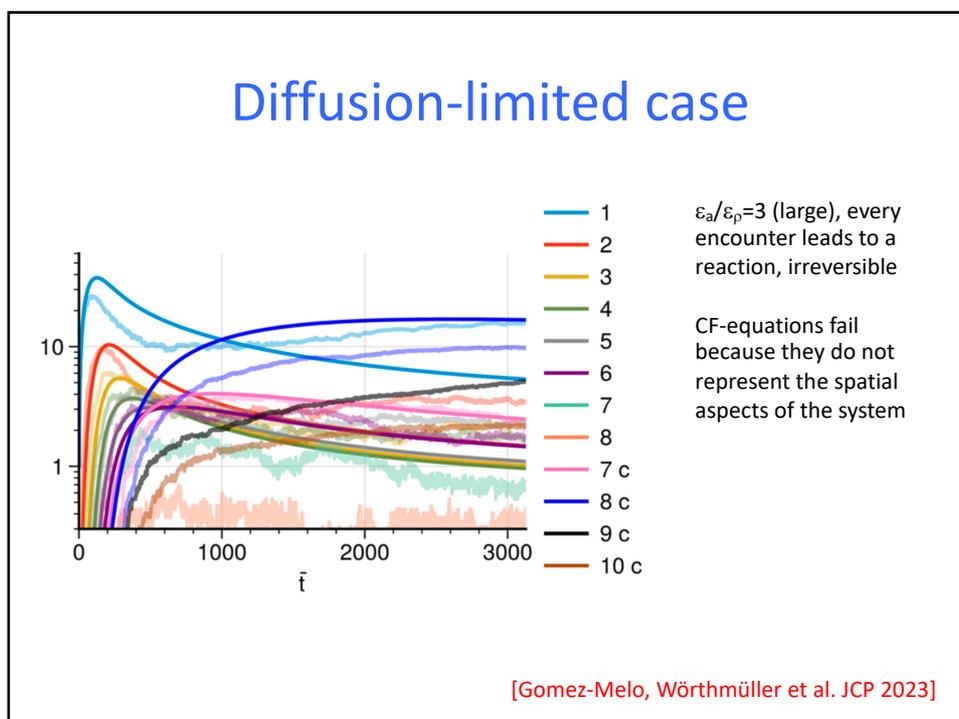
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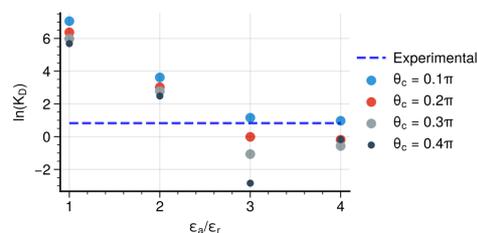


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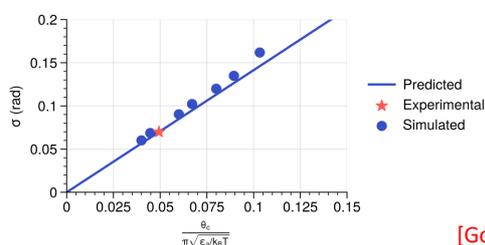


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Comparison with experiments



K_D decreases with interaction energy and then comes flat (diffusion-limited). Experiments suggest $2 < E_a/E_r < 3$. From selectivity one estimates $0.1\pi < \theta_c < 0.2\pi$

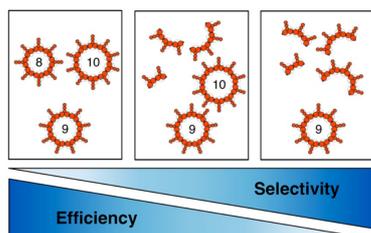


Bond angle fluctuations are an Ornstein-Uhlenbeck process (straight line). Experiments with $\sigma=4$ deg suggest $\theta_c = 0.17\pi$ (31 deg)

[Gomez-Melo, Wörthmüller et al. JCP 2023]

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Competition between efficiency and selectivity



Target Function L

E_a/E_r	0.1	0.2	0.3	0.4
4	0.83	0.576	0.595	0.612
3	0.812	0.622	0.675	0.699
2	0.826	0.847	0.782	0.735

θ_c/π

The SAS-6 system cannot achieve both efficiency (due to high reversibility avoiding kinetic trapping) and selectivity (selection of the 9-ring) at the same time, but has to balance these two targets (green frame). Additional molecular mechanisms for 9-ring selection must exist.

[Gomez-Melo, Wörthmüller et al. JCP 2023]

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Summary

- SAS-6 dimers forms 9-fold rings that can be observed with HS-AFM on mica surfaces
- The surface shifts the binding equilibrium up by four orders of magnitude compared to bulk, by concentrating the molecules
- This explains why daughter centrioles form on the surface of mother centrioles
- Due to the fast kinetics, the assembly curves can be fitted by the coagulation-fragmentation (CF) model
- Frequent dissociation avoids kinetic traps and leads to successful assembly, similar to the situation with viruses
- The comparison between reaction kinetics (CF-equations) and spatial simulations (Brownian Dynamics) showed the limits of the kinetic approach: spatial effects would be more important if interaction energies were higher
- Like for viruses, malformed structures can form (7-, 8-, 10-rings, squeelices)
- The simulations reveal the intrinsic challenge to balance efficiency and selectivity and suggests that additional molecular mechanisms must exist in the cell to select the 9-fold rings (similar to scaffolding proteins like P22 for viruses)

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Acknowledgements



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Conference announcements



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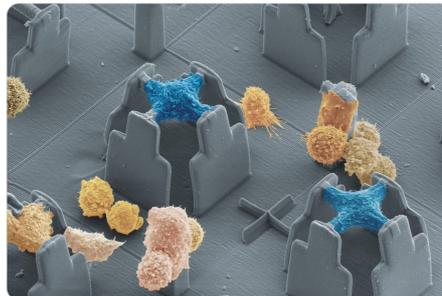


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