

# Controlling capsid assembly with antivirals and liquid-liquid phase separation

Michael F. Hagan

**Farri Mohajerani**

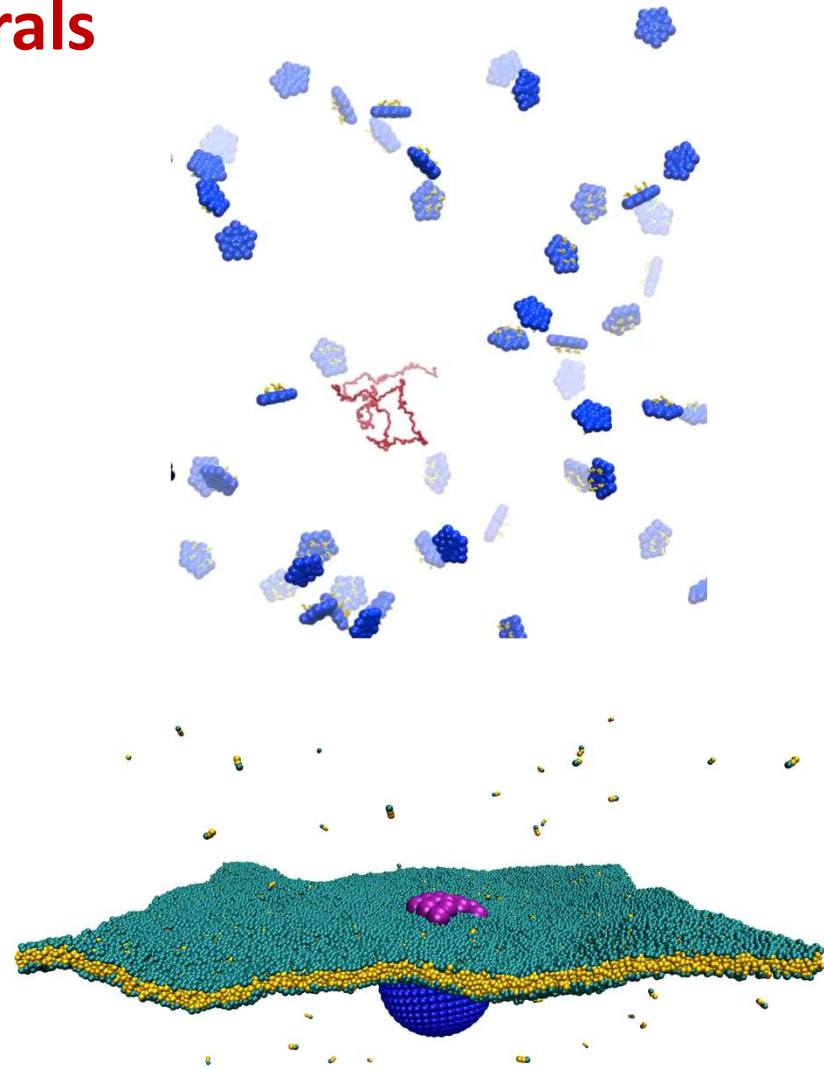
Naren Sundararajan

Department of Physics and  
Quantitative Biology Program,  
Brandeis University

**Jodi Hadden-Perilla (U. Delaware)**

**Chris Schlicksup, Adam Zlotnick (Indiana University)**

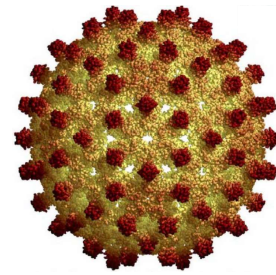
Brandeis  
bioinspired  
**MRSEC**



# Understanding and controlling capsid self-assembly

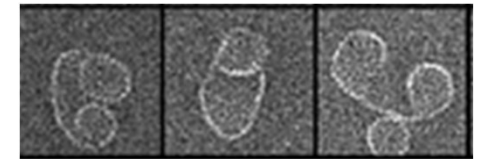
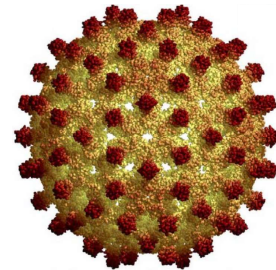
1. What factors control assembly pathways and outcomes

Example: HBV capsids form T=3 and T=4 shells



2. Can we design molecules to redirect assembly to different sizes or morphologies?

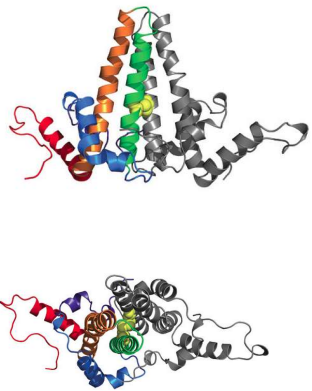
Example: HBV antivirals



3. Coupling to liquid-liquid phase separation (biomolecular condensates) can change assembly rates by orders of magnitude and make it more robust

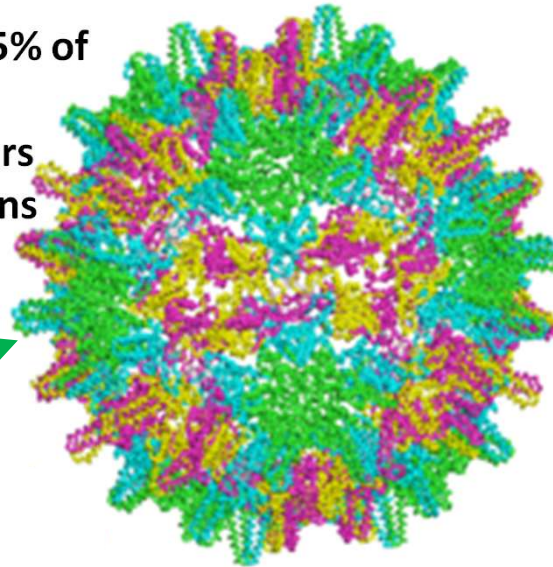
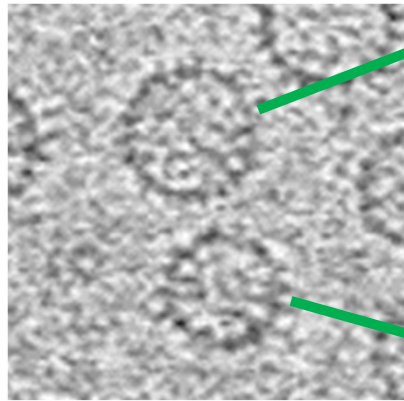
# HBV capsid (core) comes in 2 sizes

## HBV core protein dimer

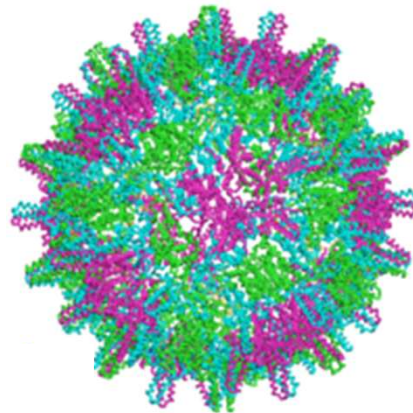


**T=4 Capsid (infectious, 95% of assemblies)**

120 core protein dimers  
4 protein conformations



**T=3 Capsid (5%)**  
90 core protein dimers  
3 protein conformations

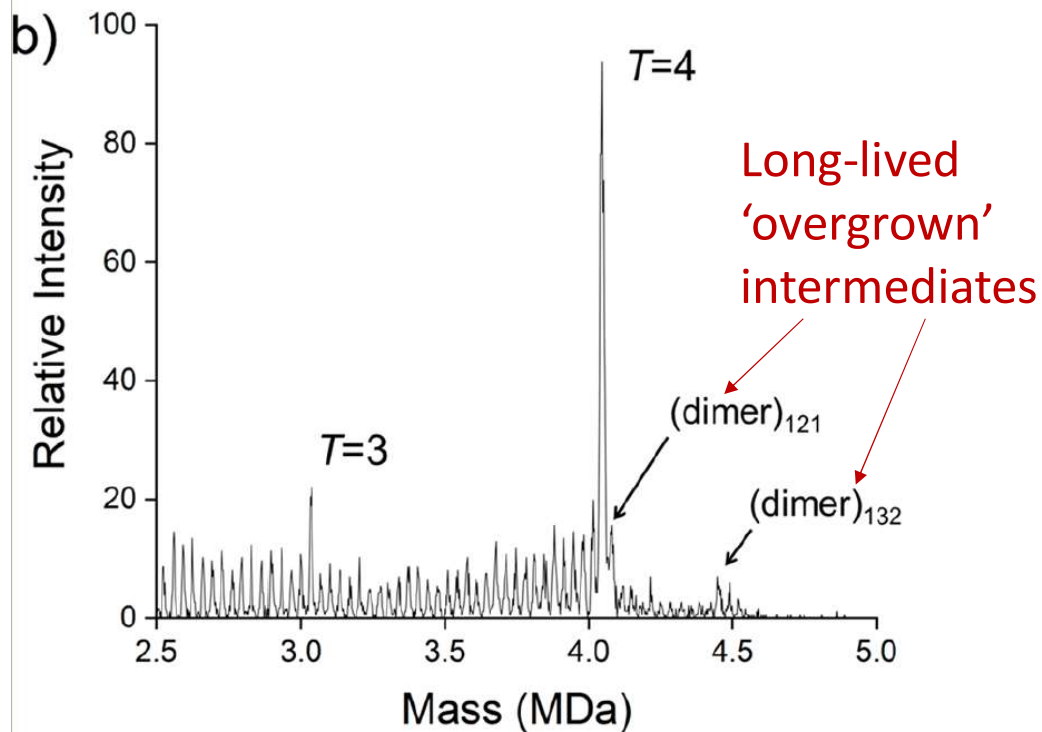


Different colors indicate different protein conformations  
see Caspar & Klug (1962), *Cold Spring Harb Symp Quant Biol* 1962;27:1-24. doi: 10.1101/sqb.1962.027.001.005)

# Experiments on HBV assembly

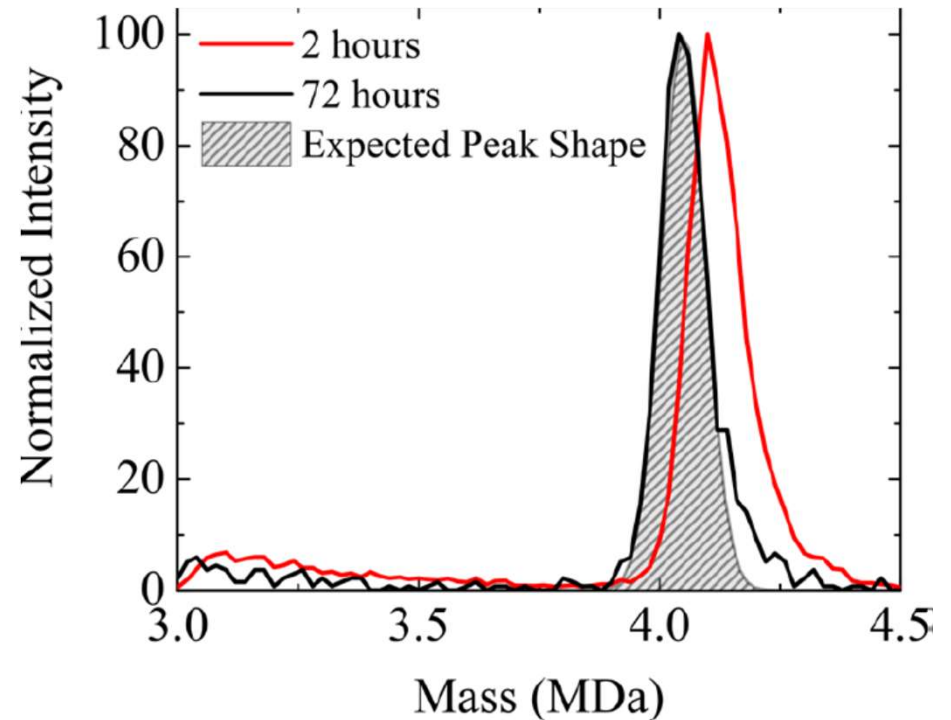
Charge Detection Mass Spec (CDMS) measures capsid sizes with single-dimer resolution

## CDMS of human HBV



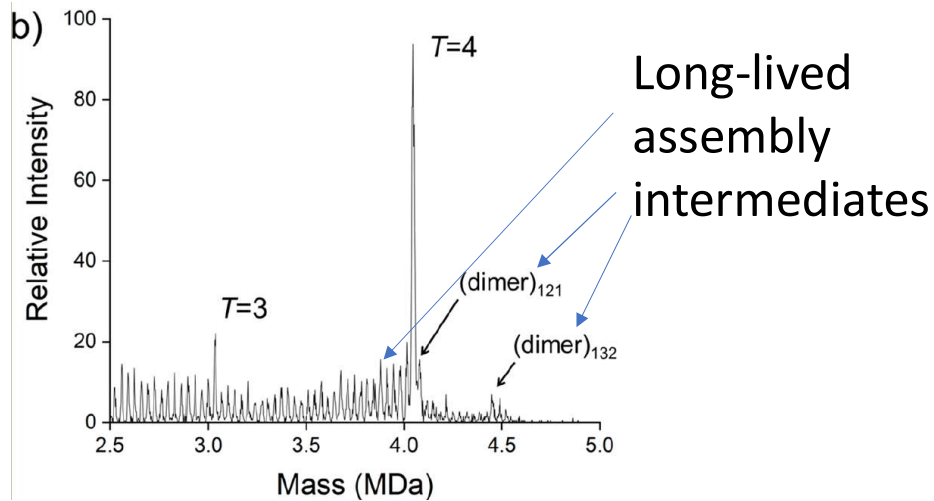
Todd, Barnes, Young, Zlotnick, Jarrold, *Anal. Chem.* **92**, 11357 (2020)

Capsids assemble overgrown intermediates before forming  $T=4$  capsid

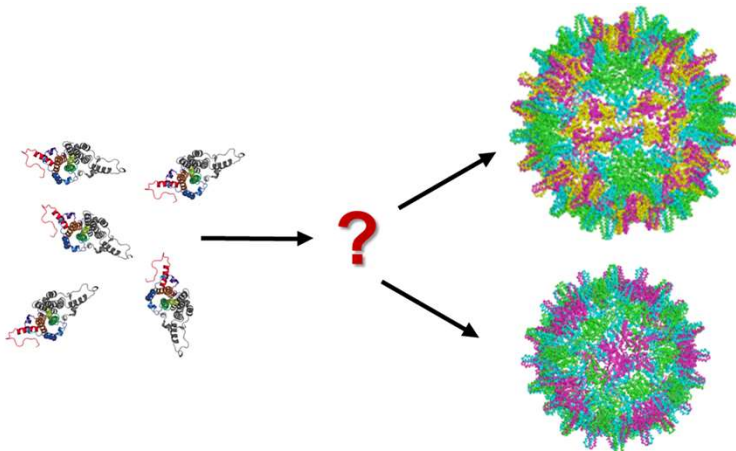
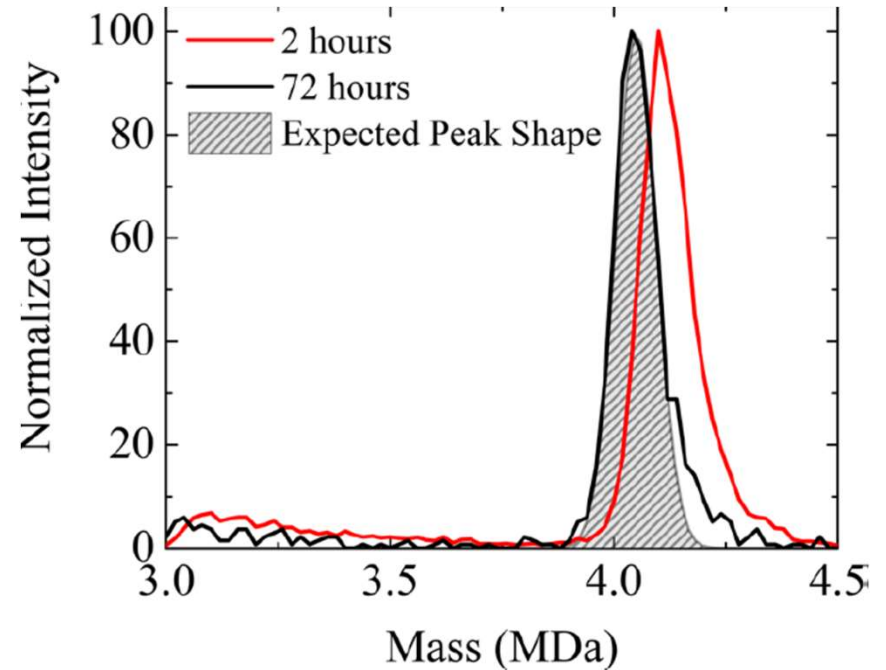


Lutomski, Lykтей, Zhao, Pierson, Zlotnick, Jarrold, *JACS*, **139**, 16932 (2017)

# Experiments on HBV assembly



Todd, Barnes, Young, Zlotnick, Jarrold, *Anal. Chem.* **92**, 11357 (2020)

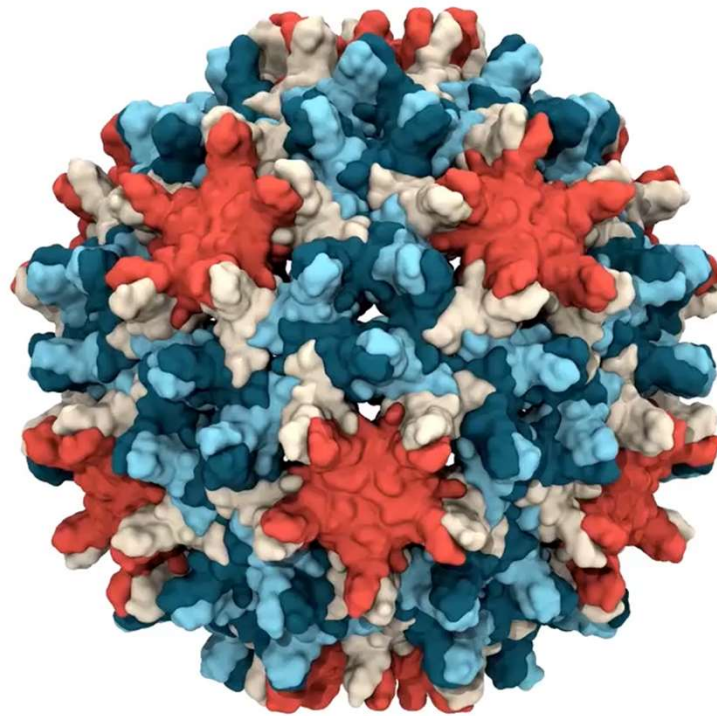


**Experiments can't resolve structures of intermediates along assembly pathways or overgrown intermediates**

# All-Atom simulations of HBV

All-atom simulation of complete (but empty) HBV capsid,  $\sim 1 \mu\text{s}$

Jodi Hadden  
et al., eLife  
(2018)



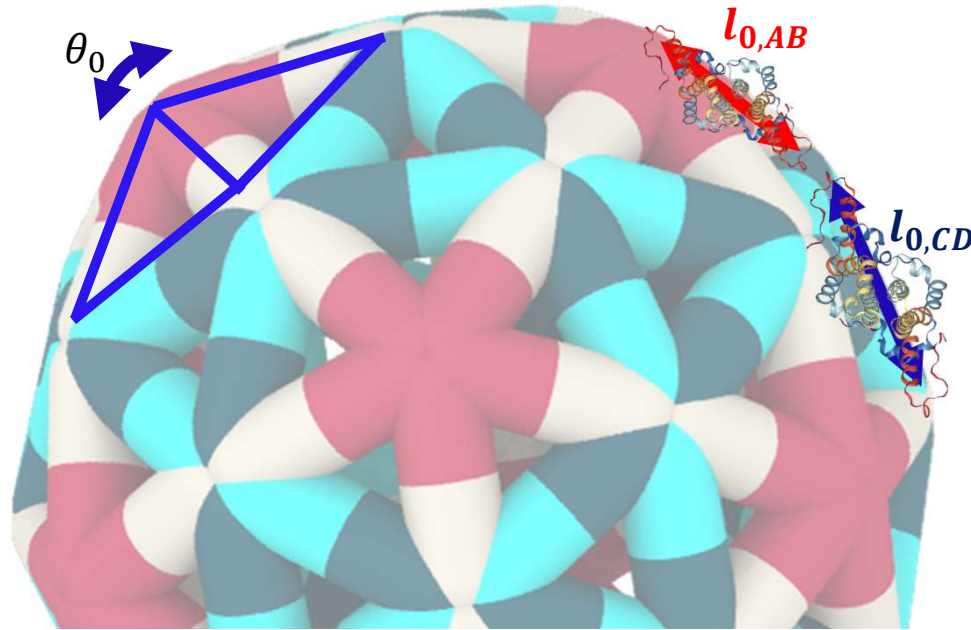
Not yet tractable to  
simulate **assembly**  
with all-atom  
simulations

**We need a model that can link all-atom simulations and experimental data  
with assembly dynamics**

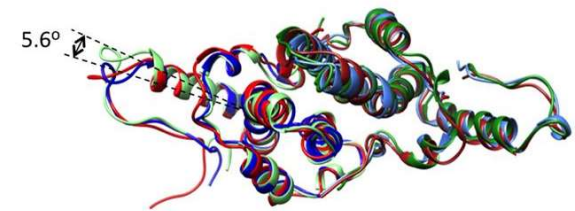


# Computational model

capsid = elastic network with edges corresponding to protein dimers



dimers have two conformations: **AB** and **CD**



Mohajerani et al. ACS Nano (2022)

adapted from:  
 -GM Rotskoff, PL Geissler, PNAS (2018)  
 -Panahandeh, Li, Marichal, Rubim, Tresset, Zandi, ACS Nano (2020)  
 -Tyukodi, Mohajerani, Hall, Grason, Hagan, ACS Nano (2021)

$$G_{\text{elastic}} = \sum_{i=\text{edges}} \kappa_l / 2 (l_i - l_0)^2 + \kappa_\theta / 2 (\theta_i - \theta_0)^2 + \dots$$

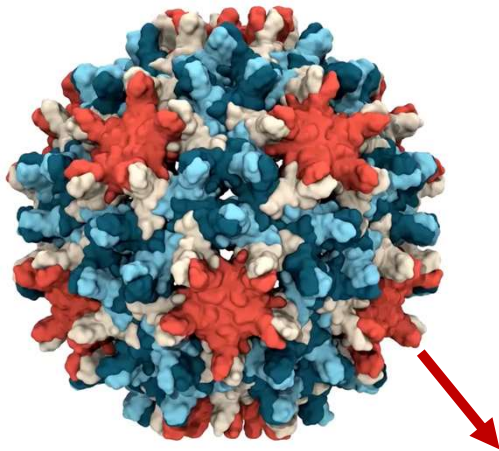
$\kappa_l \rightarrow$  Young's modulus (stretching)  
 $\kappa_\theta \rightarrow$  bending modulus

simulate assembly with dynamical Monte Carlo

# Estimating model parameters from all-atom simulations

Optimize model parameters so that distributions of edge lengths and angles in coarse-grained simulation matches all-atom

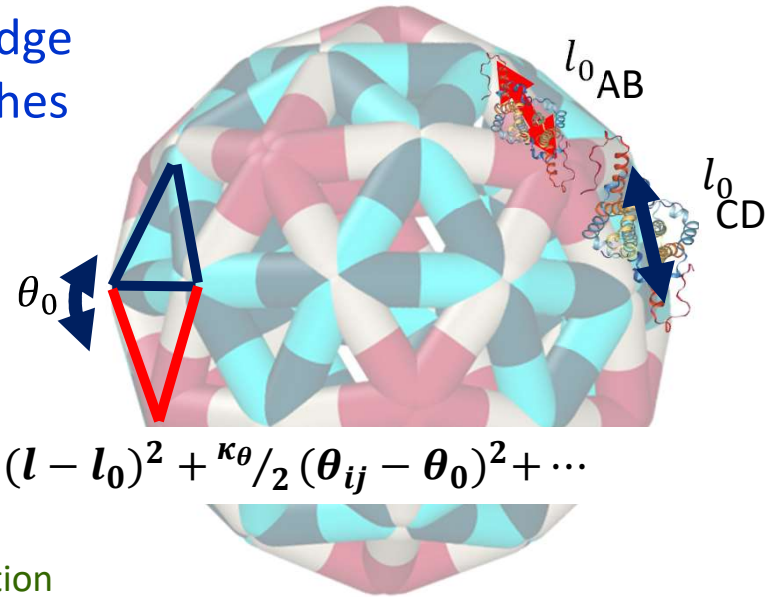
fit parameters:  $\kappa_l, \kappa_\theta, \kappa_\phi, l_{0,AB}, l_{0,CD}, \theta_{0,AB}, \theta_{0,CD}, \dots$



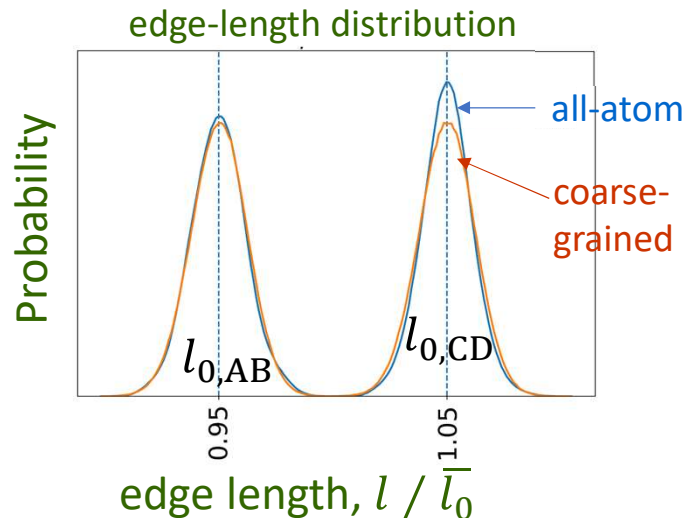
Jodi Hadden et. al., eLife (2018)

$$\kappa_l = 4200 \frac{k_B T}{\bar{l}_0}, \kappa_\theta = 40 k_B T$$

Föppl-von Kármán # = 500



$$G_{\text{elastic}} = \kappa_l / 2 (l - l_0)^2 + \kappa_\theta / 2 (\theta_{ij} - \theta_0)^2 + \dots$$

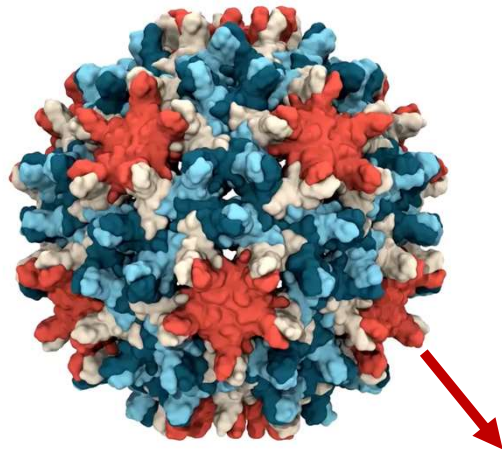




# Estimating model parameters from all-atom simulations

Optimize model parameters so that distributions of edge lengths and angles in coarse-grained simulation matches all-atom

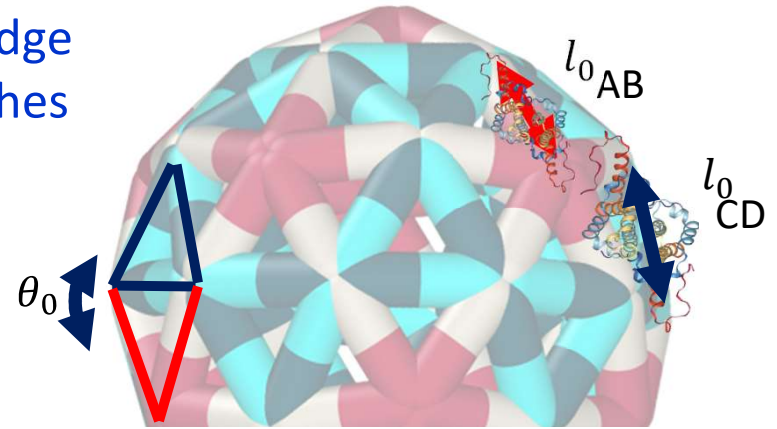
fit parameters:  $\kappa_l, \kappa_\theta, \kappa_\phi, l_{0,AB}, l_{0,CD}, \theta_{0,AB}, \theta_{0,CD}, \dots$



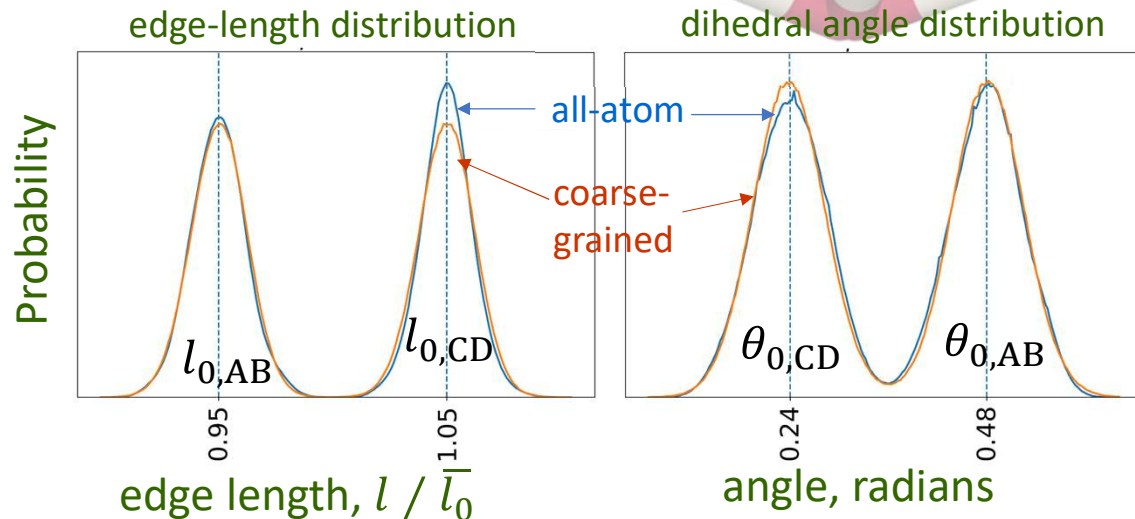
Jodi Hadden et. al., eLife (2018)

$$\kappa_l = 4200 \frac{k_B T}{\bar{l}_0}, \kappa_\theta = 40 k_B T$$

Föppl-von Kármán # = 500



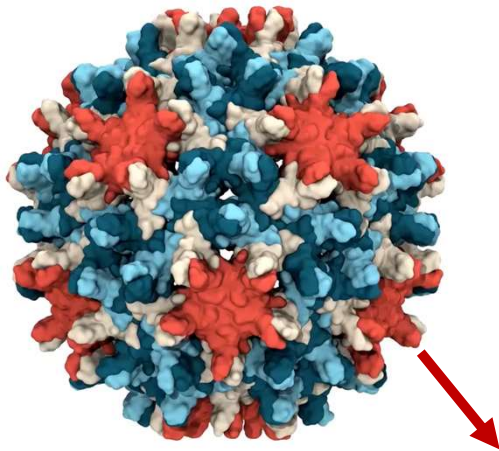
$$G_{\text{elastic}} = \frac{\kappa_l}{2} (l - l_0)^2 + \frac{\kappa_\theta}{2} (\theta_{ij} - \theta_0)^2 + \dots$$



# Estimating model parameters from all-atom simulations

Optimize model parameters so that distributions of edge lengths and angles in coarse-grained simulation matches all-atom

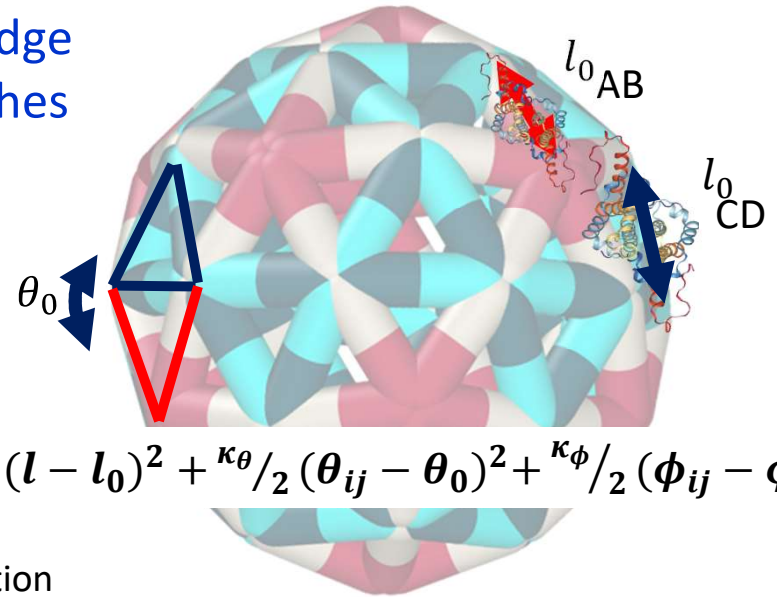
fit parameters:  $\kappa_l, \kappa_\theta, \kappa_\phi, l_{0,AB}, l_{0,CD}, \theta_{0,AB}, \theta_{0,CD}, \dots$



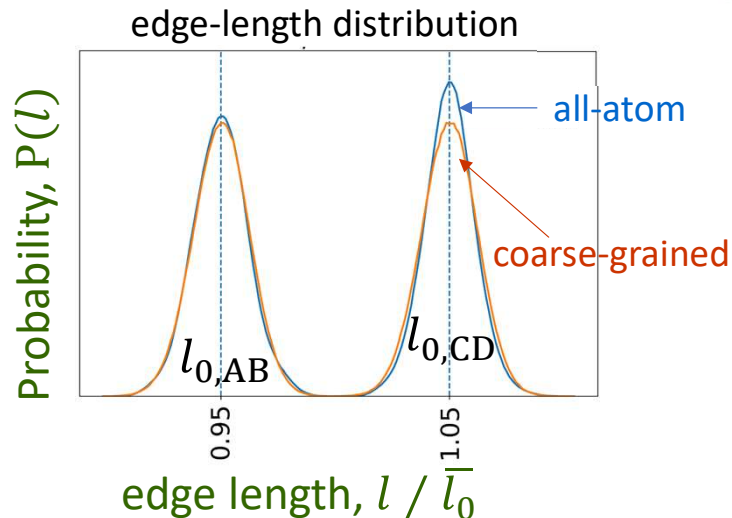
Jodi Hadden et. al., eLife (2018)

$$\kappa_l = 4200 \frac{k_B T}{l_0}, \kappa_\theta = 40 k_B T$$

Föppl-von Kármán # = 500



$$G_{\text{elastic}} = \kappa_l / 2 (l - l_0)^2 + \kappa_\theta / 2 (\theta_{ij} - \theta_0)^2 + \kappa_\phi / 2 (\phi_{ij} - \phi_0)^2$$



previous models have only 1 conformation, cannot fit all-atom data

need 2 subunit types ('ultra-coarse graining'):

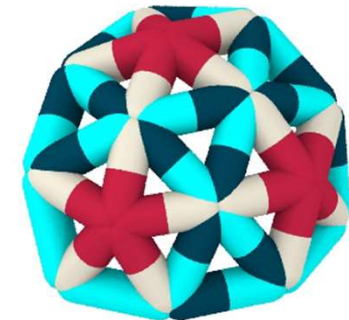
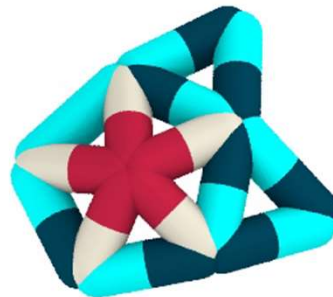
Elrad&MFH, Nanolett (2008); Grime, ..., Voth Nat. Comm. (2016); Dama, Jin, Voth JCTC (2017)

# Subunit association/dissociation/relaxation

adapted from: GM Rotskoff, PL Geissler, PNAS (2018)  
Panahandeh, Li, Marichal, Rubim, Tresset, Zandi, ACS Nano (2020)  
Tyukodi, Mohajerani, Hall, Grason, Hagan, ACS Nano (2021)

Addition of one edge  
Removal of one edge

Addition of two edges  
Removal of two edges



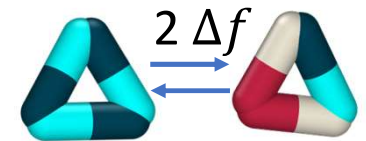
Relaxation of the shell  
between addition/removal moves

- Monte-Carlo moves are reversible  $\rightarrow$  a well-defined equilibrium distribution
- Monte-Carlo moves mimic real dynamics (hopefully)
- dimer-dimer binding affinities for different conformations estimated from buried surface area

2 control parameters (depend on [salt], pH, temperature)

- mean subunit-subunit binding affinity,  $g_b$

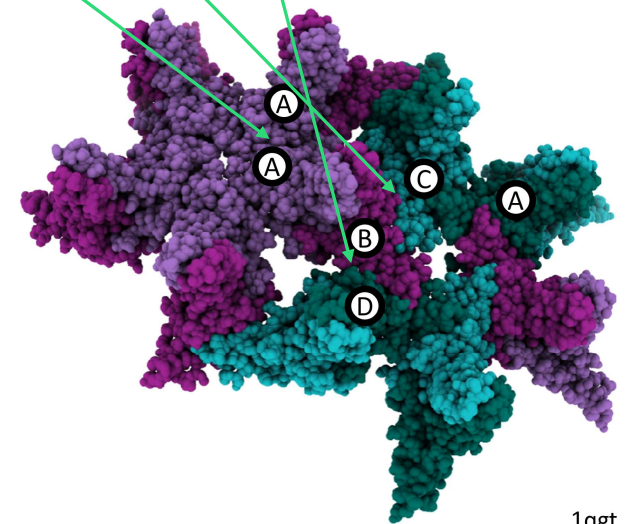
- Equilibrium ratio AB/CD dimer conformations,  $K_{AB} = \frac{[AB]}{[CD]} = \exp\left[-\Delta f/k_B T\right]$



# Subunit conformations

Estimate relative dimer/dimer binding affinities from buried surface area (PDBePISA)

AA/CD	BC/CD	DB/DC
1.3	1.1	0.9



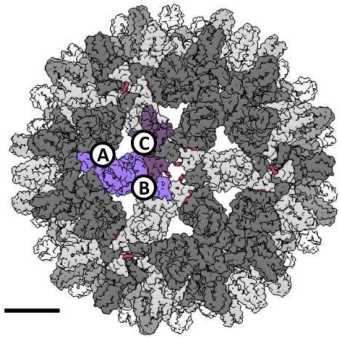
1qgt

- Monte-Carlo moves are reversible → a well-defined equilibrium distribution
- Monte-Carlo moves mimic real dynamics (hopefully)
- dimer-dimer binding affinities for different conformations estimated from buried surface area

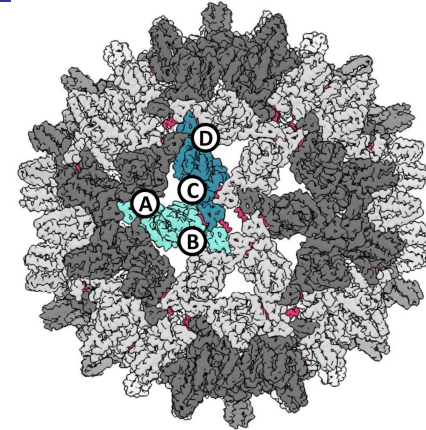
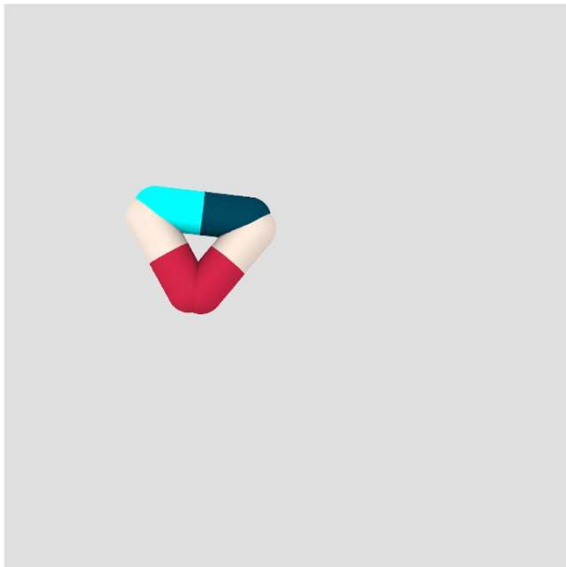
2 unknown parameters (can't estimate from atomistic simulations or structures):

- mean subunit-subunit binding affinity,  $g_b$  (depends on [salt], temperature, pH)
- Equilibrium ratio AB/CD dimer conformations,  $\frac{[AB]}{[CD]} = \exp\left[-\Delta f/k_B T\right]$

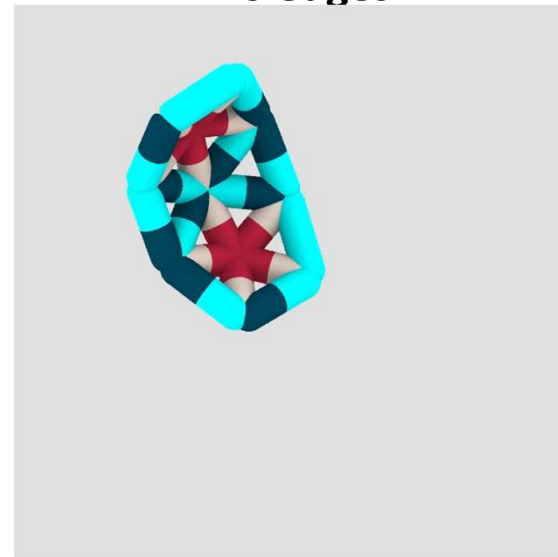
# Example simulation trajectories



90 edges (dimers)



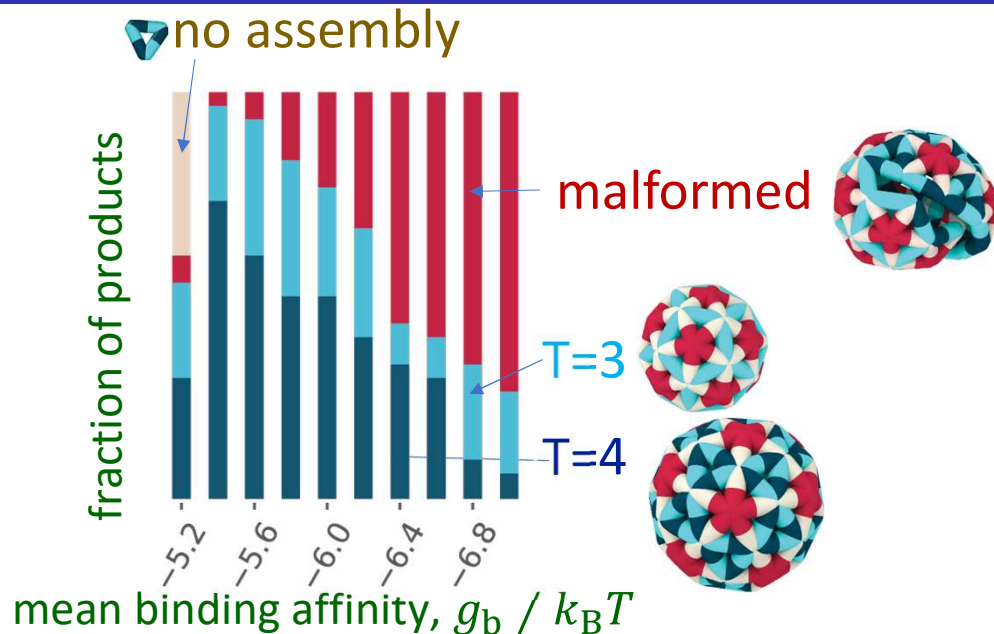
120 edges



need two  
dimer  
types to  
get T=4  
capsids

$$g_b = 6.5 k_B T$$
$$\Delta f = 3.5 k_B T$$
$$[\text{dimer}] = 10 \mu\text{M}$$

# Parameters that control assembly morphologies



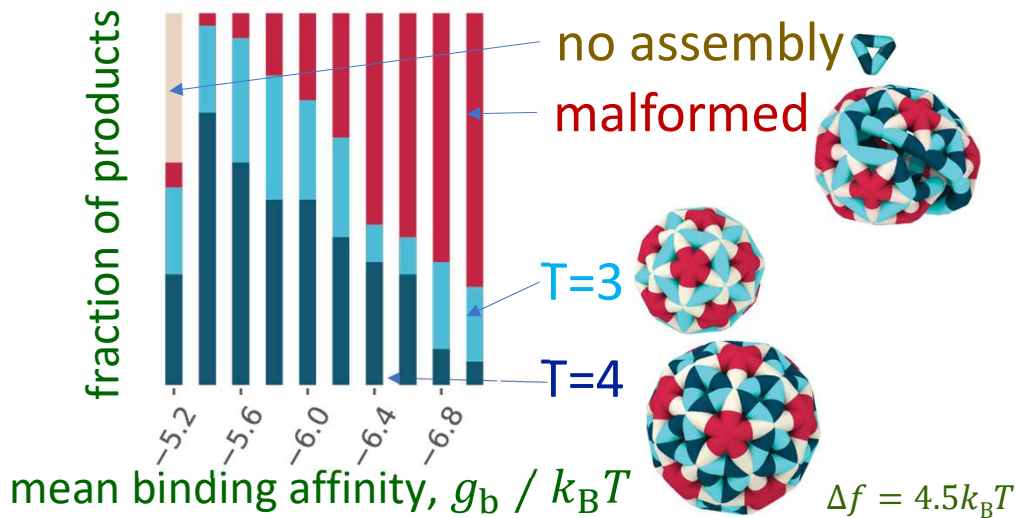
- malformed structures assemble when binding affinity too strong compared to  $k_B T$  ( $1 k_B T = 0.6 \text{ kcal/mol}$ )
- consistent with CDMS, lightscattering experiments and previous simulations
- $[T=4]/[T=3]$  ratio not sensitive to mean dimer-dimer binding affinity,  $g_b$

strong interactions lead to kinetic traps:

Ceres & Zlotnick 2002, Hagan & Chandler 2006

$$\Delta f = 3.6 k_B T$$

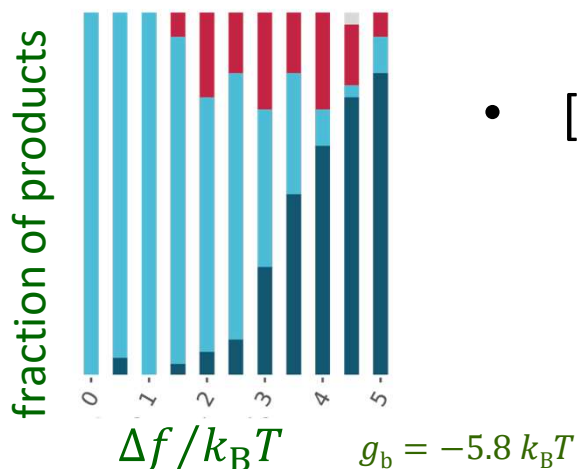
# Parameters that control assembly morphologies



- malformed structures assemble when binding affinity too strong compared to  $k_B T$  ( $1 k_B T = 0.6 \text{ kcal/mol}$ )

consistent with CDMS, lightscattering experiments, and previous simulations

- $[T=4]/[T=3]$  ratio not sensitive to mean dimer-dimer binding affinity,  $g_b$

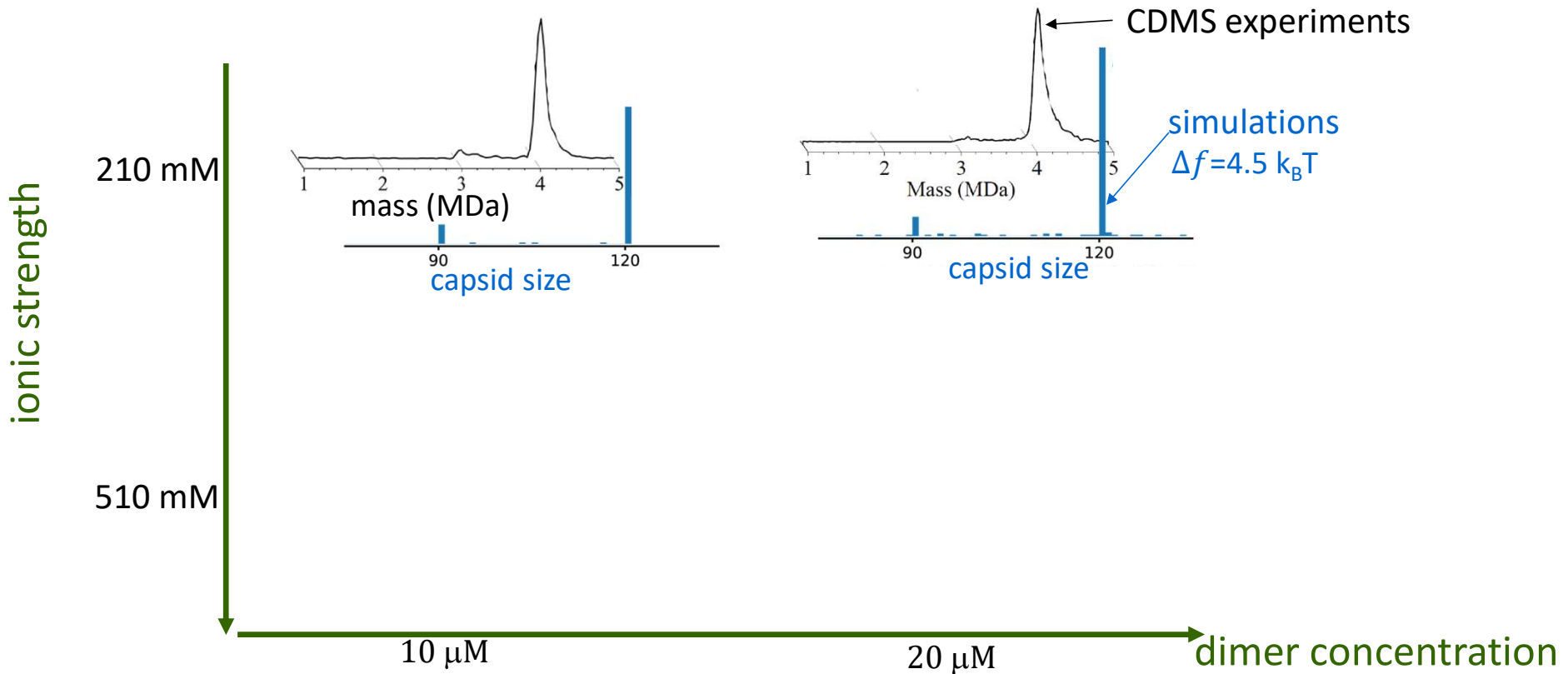


- $[T=4]/[T=3]$  ratio depends on conformational free energy landscape

$\Delta f$  = free energy difference between AB and CD dimers:

$$K_{AB/CD} = \frac{[AB]}{[CD]} = \exp\left[-\Delta f / k_B T\right]$$

# Qualitative comparison with experiments



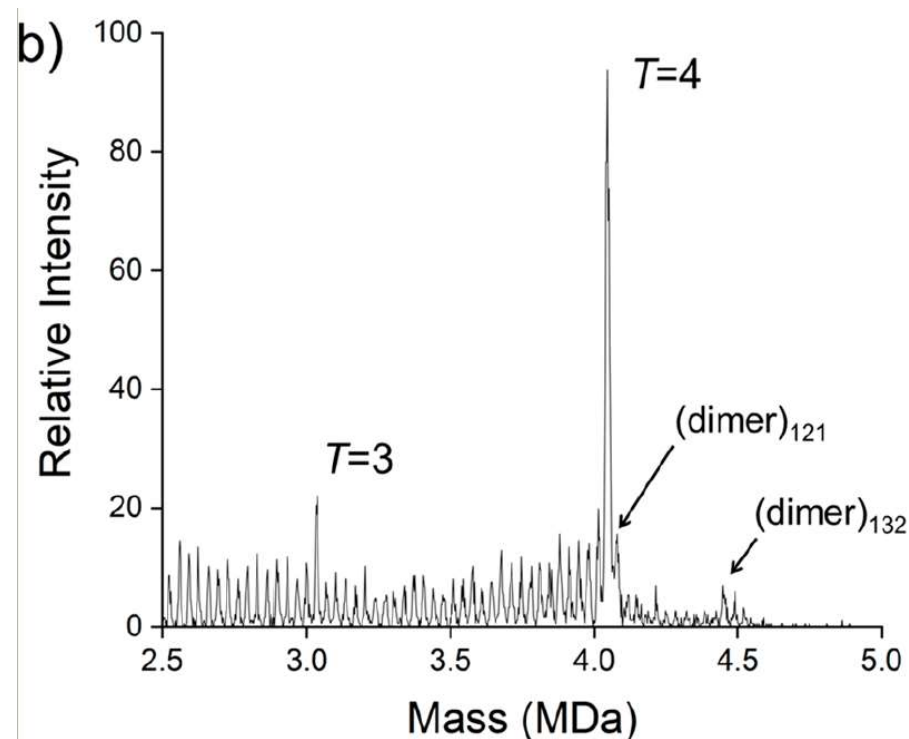
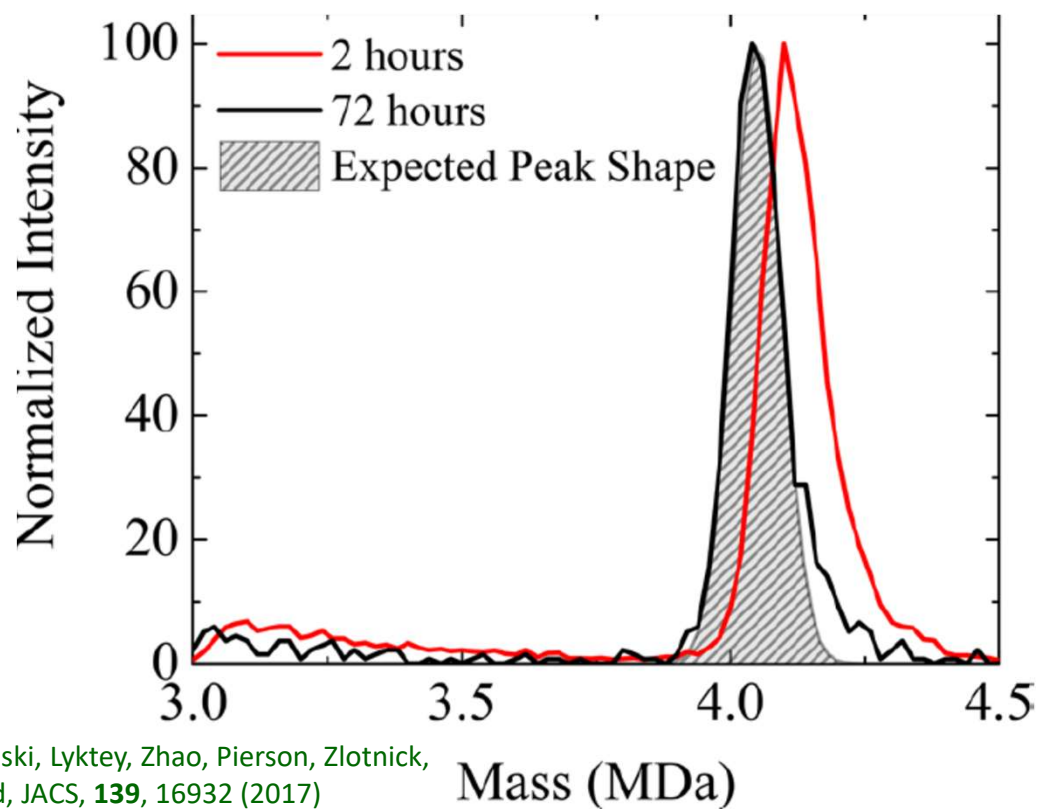
- Experiments:  $T=3/T=4$  increases with [salt] but is independent of [dimer]
- Computational results match if  $\Delta f$  decreases ( $K_{AB/CD}$  increases) with increasing [salt] (consistent with Ceres and Zlotnick, Biochemistry (2002))



## Error correction during HBV assembly (overgrown intermediates)

Charge Detection Mass Spec (CDMS) shows that HBV capsids assemble 'over-grown' intermediates before forming T=4 capsid

Long-lived 121-mer and 132-mer

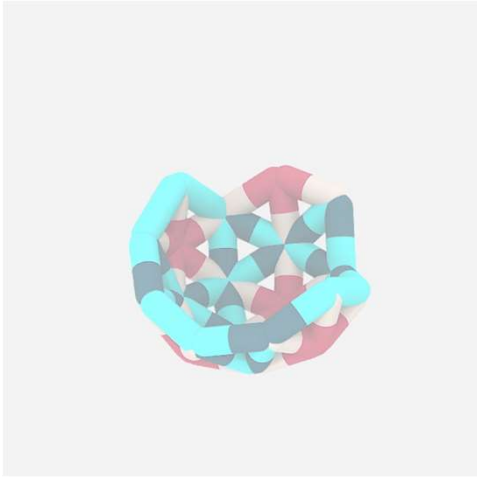


Lutomski, Lyktey, Zhao, Pierson, Zlotnick, Jarrold, JACS, **139**, 16932 (2017)

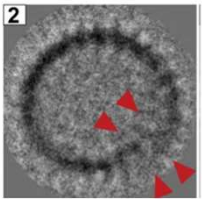
Todd, Barnes, Young, Zlotnick, Jarrold, Anal. Chem. **92**, 11357 (2020)

## Error correction during assembly

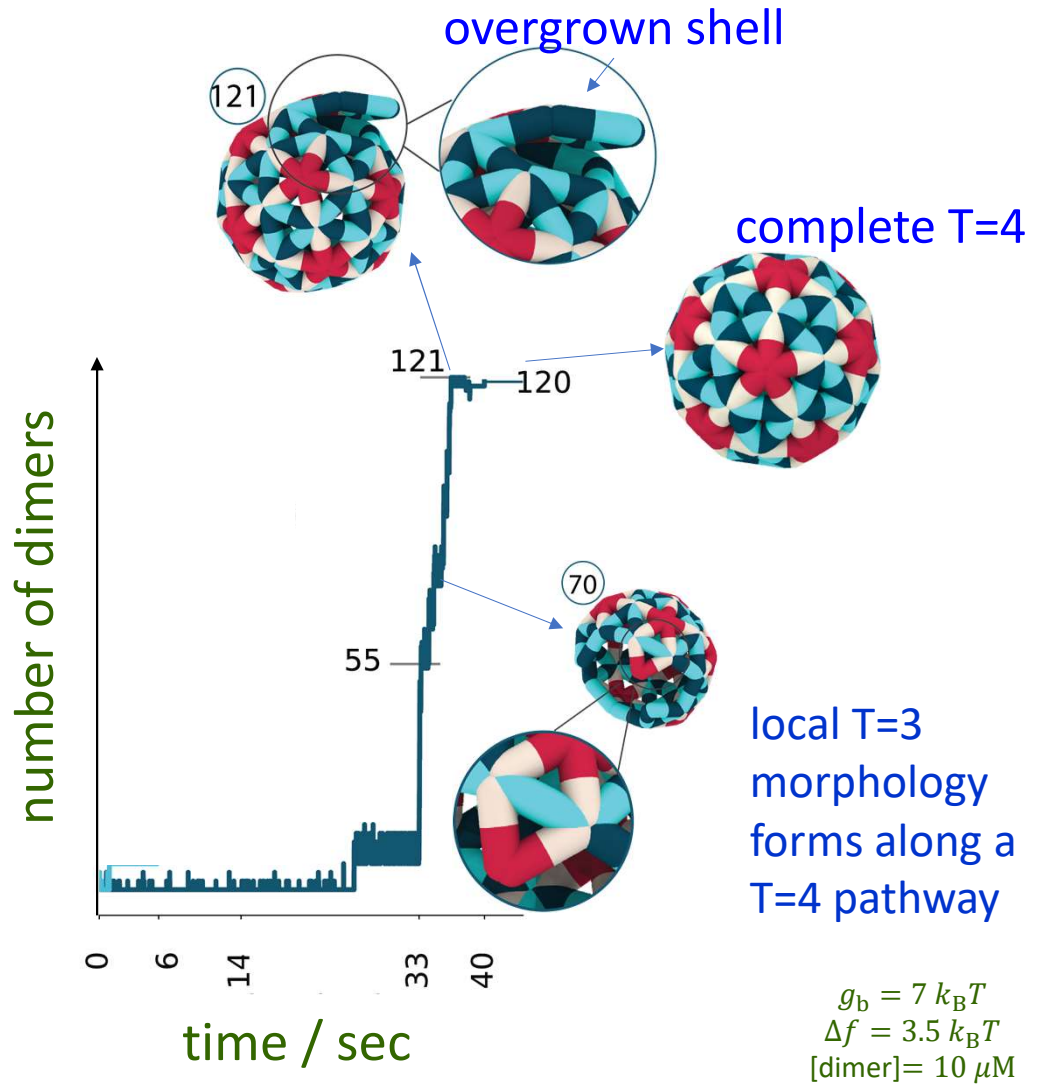
Capsid overgrows and then sheds excess subunits (as seen in experiments)



Overgrown woodchuck HBV capsids

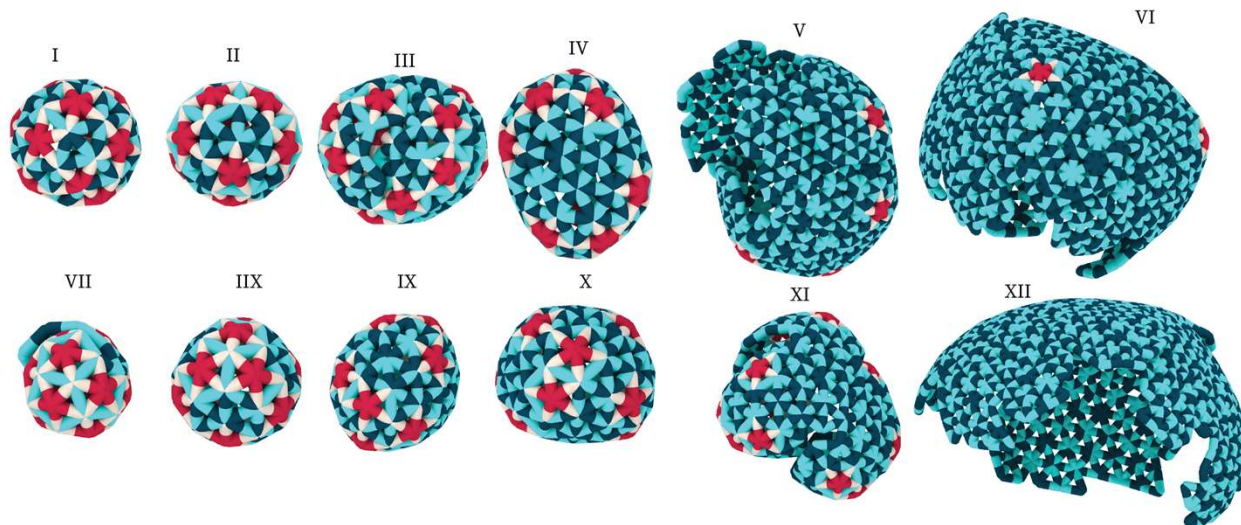
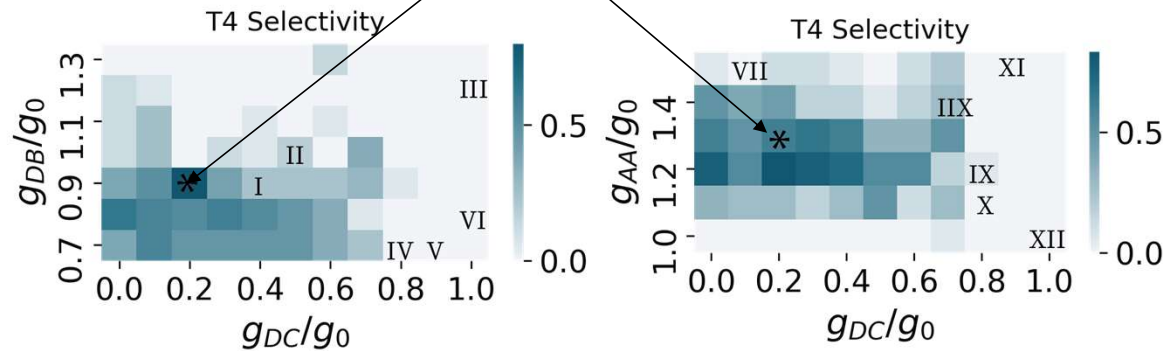


Pierson, Keifer, Kukreja, Wang, Zlotnick, Jarrold, J Mol Biol **428**, 292–300 (2016)

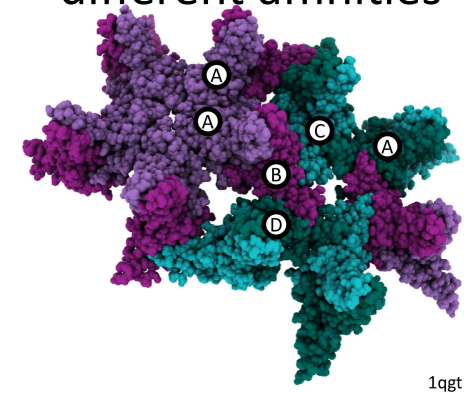


# Importance of conformational specificity

buried surface area estimate for wild-type interface affinities



different interfaces have different affinities



species-specific binding  
important design tool for  
synthetic programmable  
assemblies

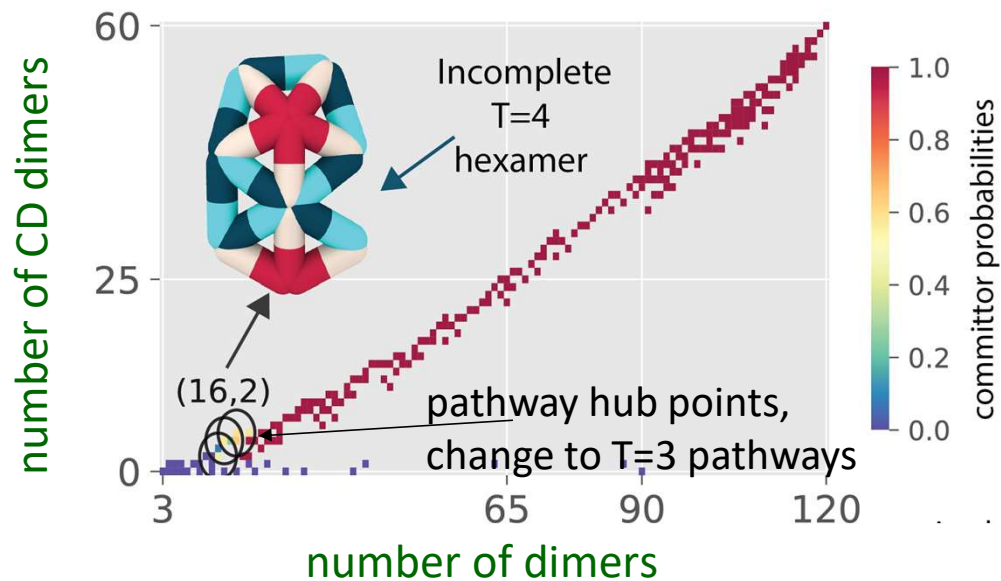
Bale et al. Science (2016)  
<https://doi.org/10.1126/science.aaf8818>;  
Sigl et al Nat. Mater. 2021; Videbæk et al,  
arXiv:2111.04717 (2021)

Mohajerani et al. ACS Nano (2022)

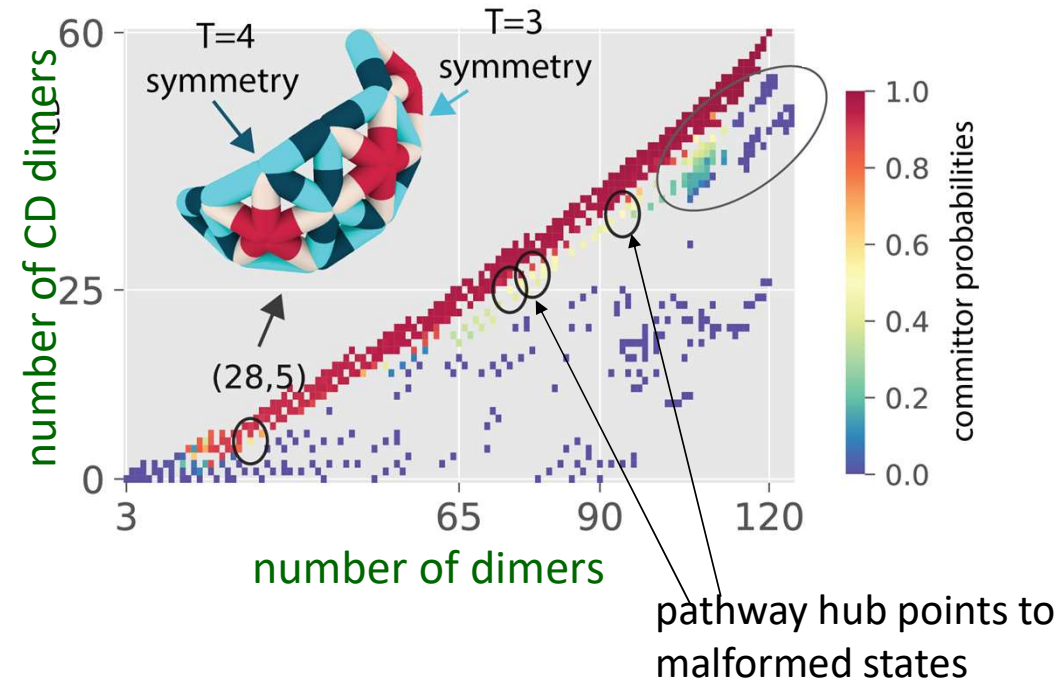
# Pathway analysis

'committer probability' = conditional probability that a structure will end up in a T=4 capsid

dimer concentration,  $C=10 \mu\text{M}$

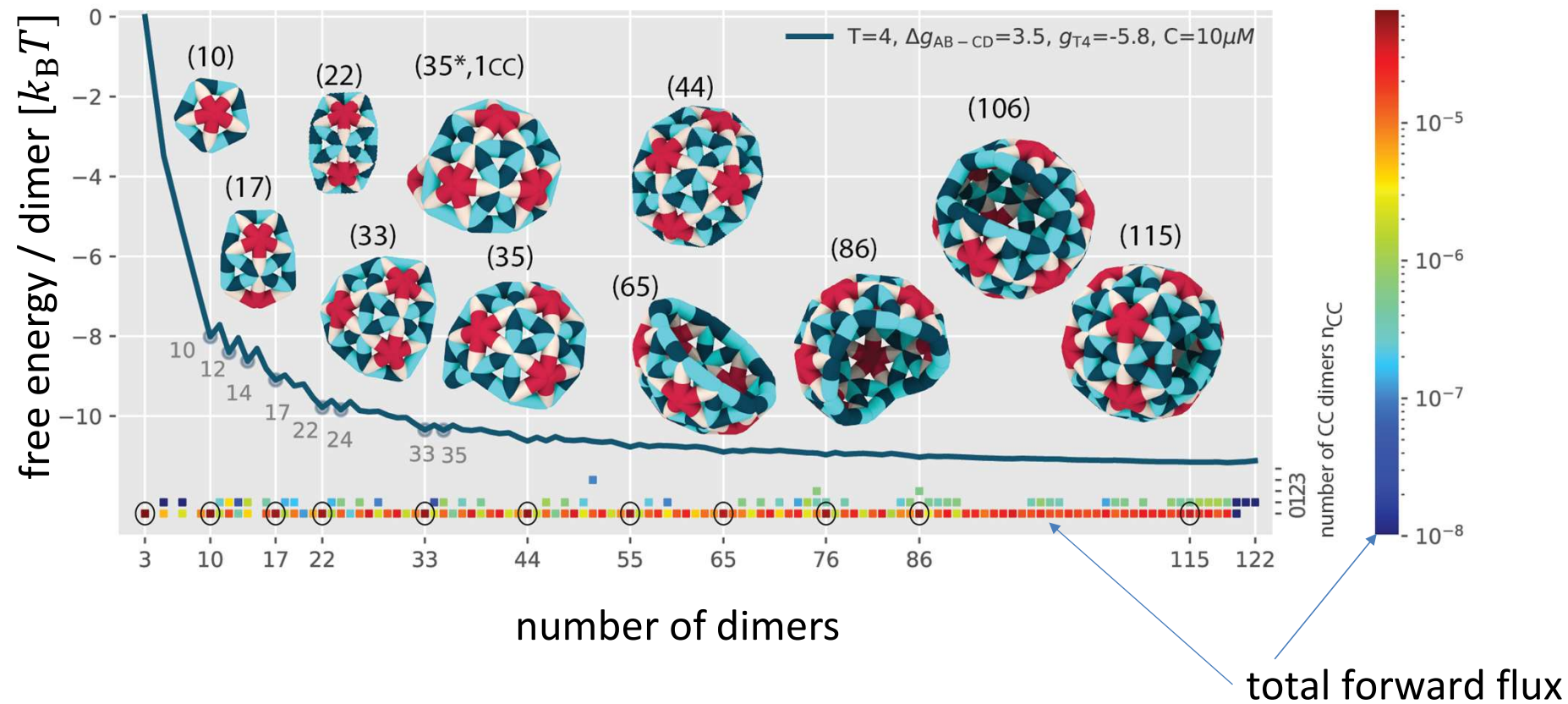


$C=20 \mu\text{M}$

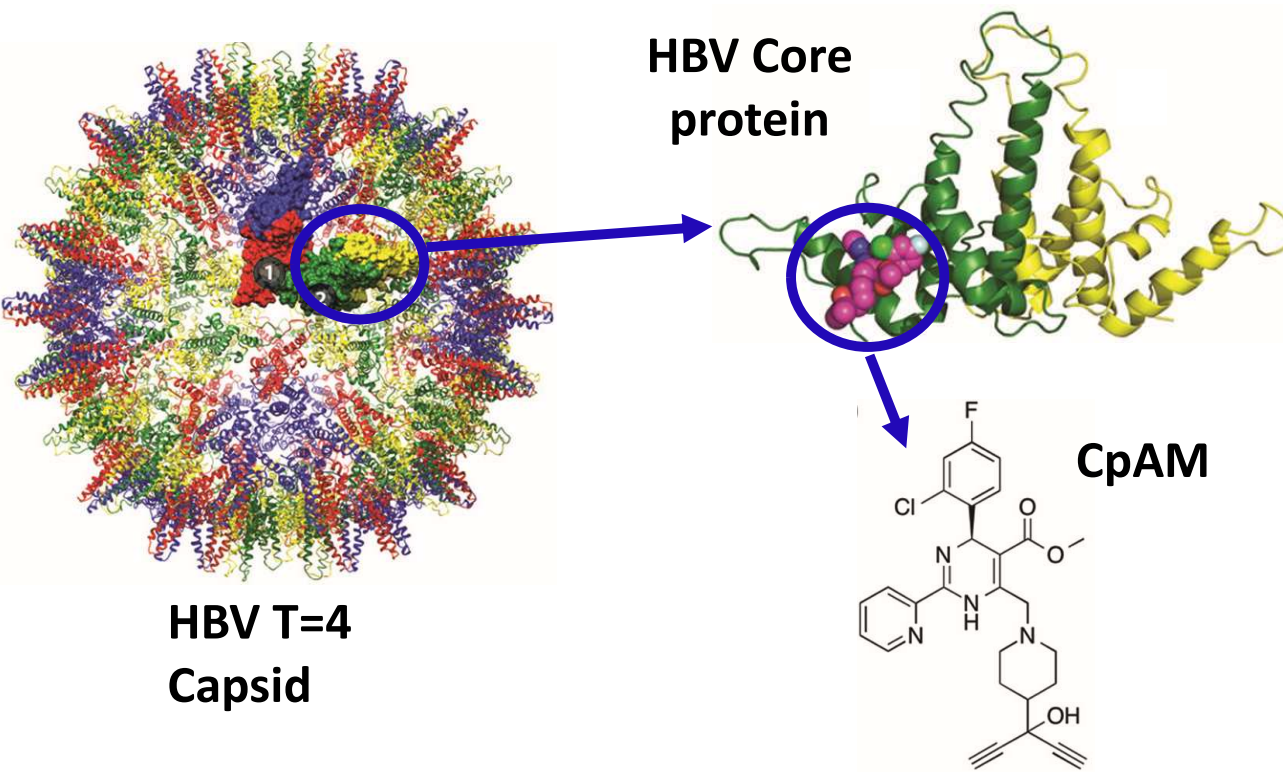


pathways can diverge to malformed pathways at large sizes with higher concentration

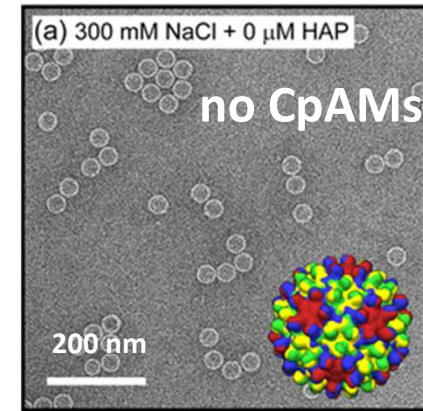
# Prevalent intermediates



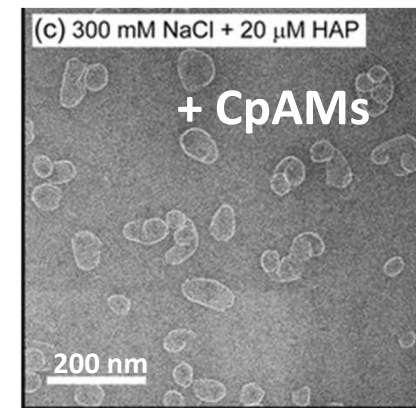
# Antiviral Agents: Core protein Allosteric Modulators (CpAMs)



**CpAMs bind to core proteins during assembly, resulting in aberrant structures.**



Adam Zlotnick

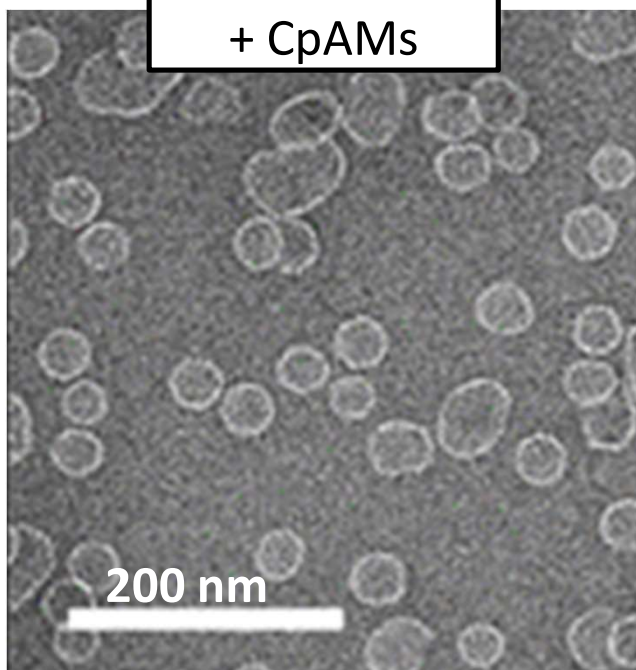


Schlicksup, C. J. , et al. Elife 7 (2018)  
Kondylis, P., et al. JACS (2018)

# In Vitro Assembly with CpAMs

Kondylis, P. , et al. *JACS* (2019)

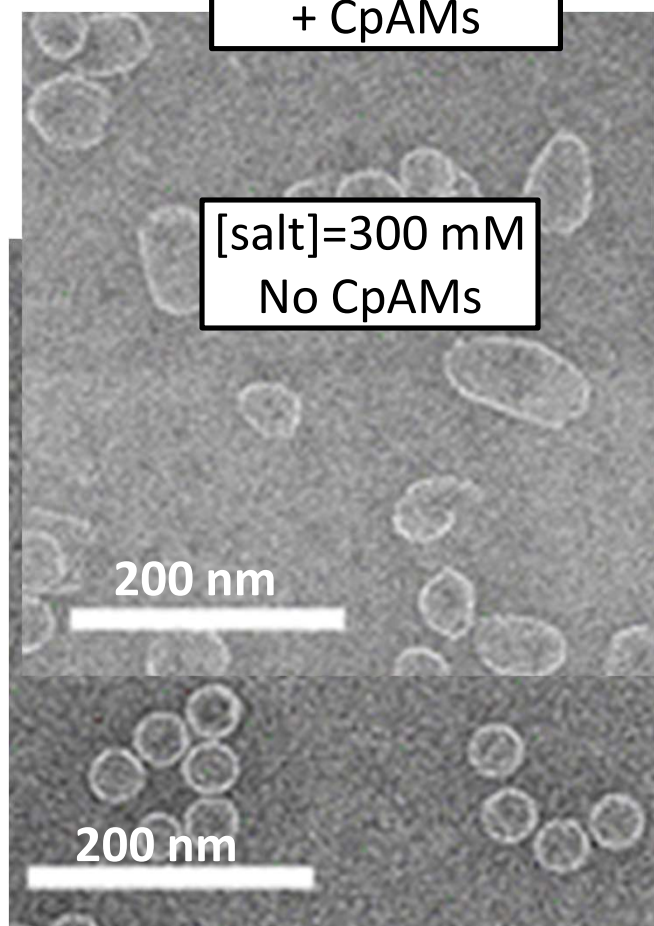
[salt]=1000 mM  
+ CpAMs



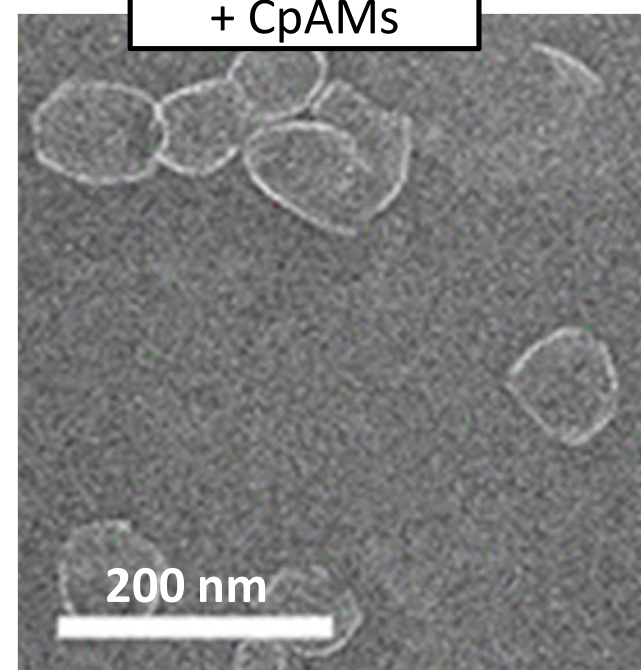
Strong protein-protein interactions:

- Higher curvature
- mostly T=4 (like native)

[salt]=300 mM  
+ CpAMs



[salt]=80 mM  
+ CpAMs

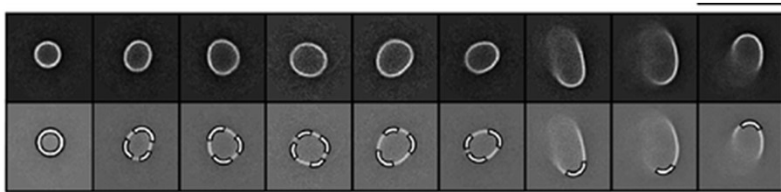


Weak protein-protein interactions:

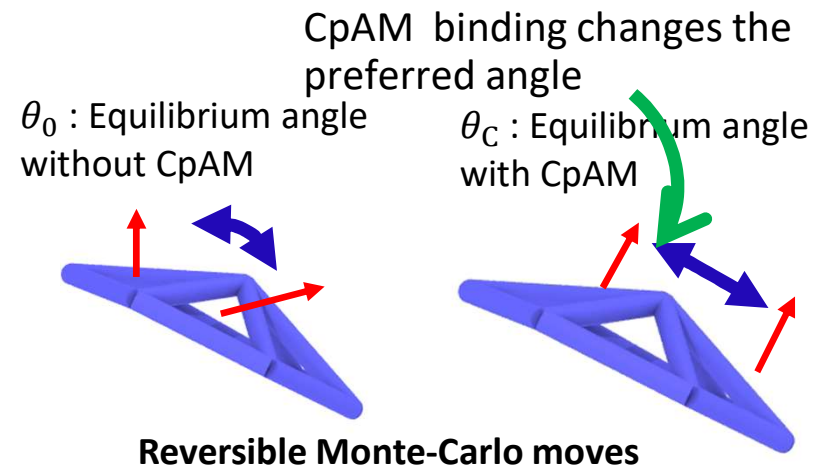
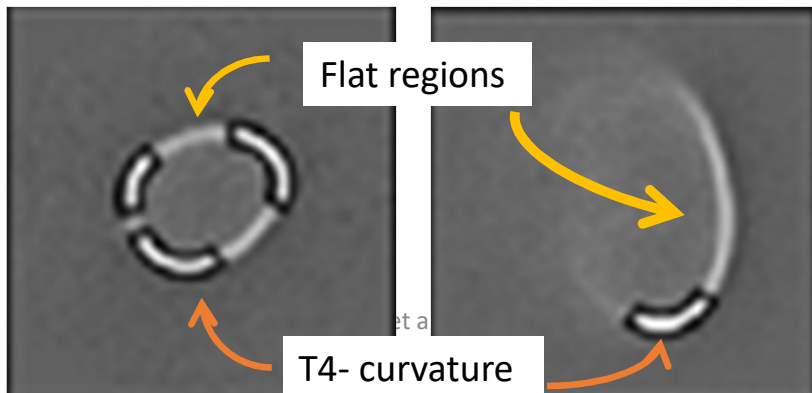
- lower curvature
- Larger, more aberrant products

# Adding CpAMs to the model

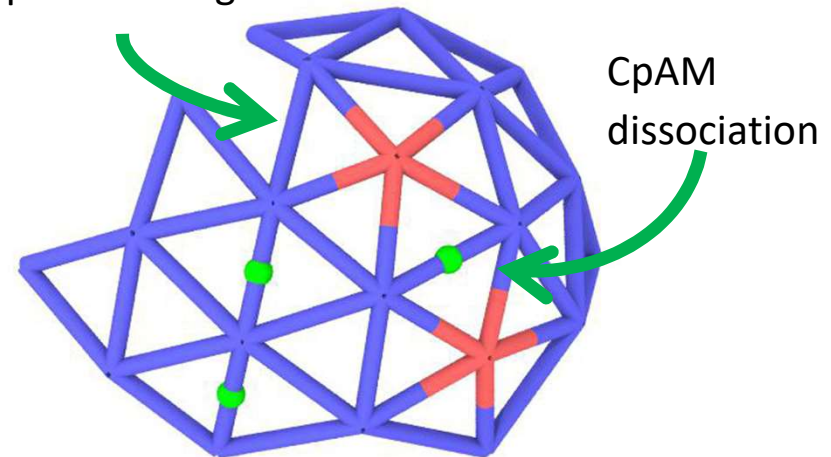
TEM of capsids assembled with CpAMs



CpAMs flatten binding angles



CpAM binding





# Simulations with CpAMs



**dimer-dimer affinity:**

$$g_b = 6.5 k_B T$$

**( moderate salt)**

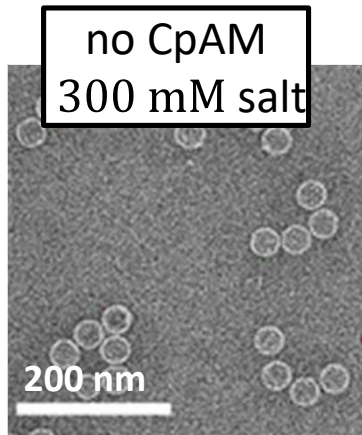


$$g_b = 16 k_B T$$

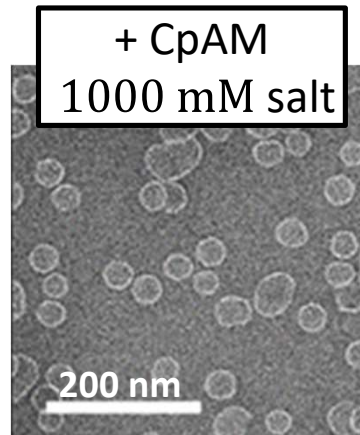
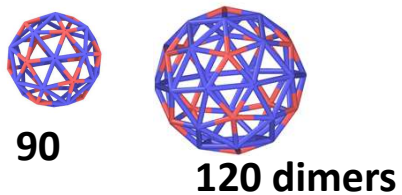
**( high salt)**

$$k_B T = 0.6 \text{ kcal/mol}$$

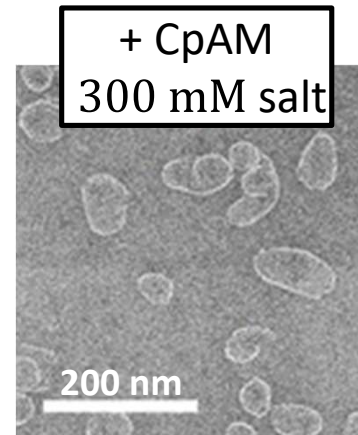
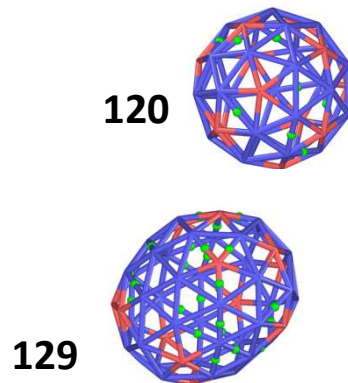
# Comparison with Experiments



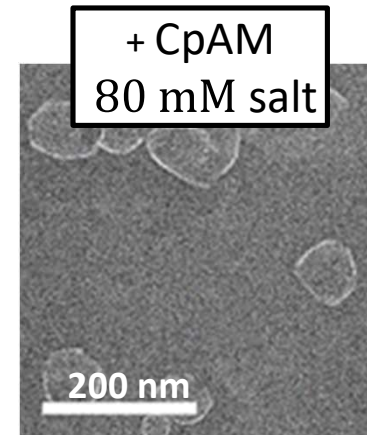
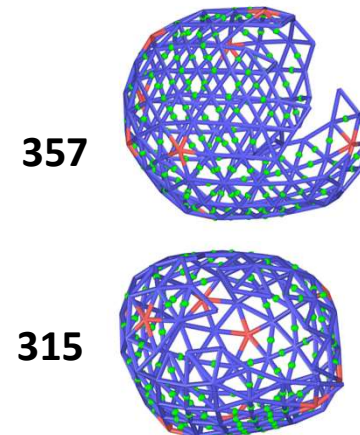
No CpAM  
 $G_{\text{bind}} = 6.5 k_B T$



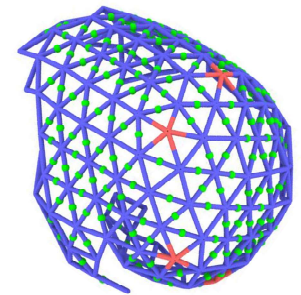
+ CpAM  
 $G_{\text{bind}} = 16.5 k_B T$



+ CpAM  
 $G_{\text{bind}} = 6.5 k_B T$

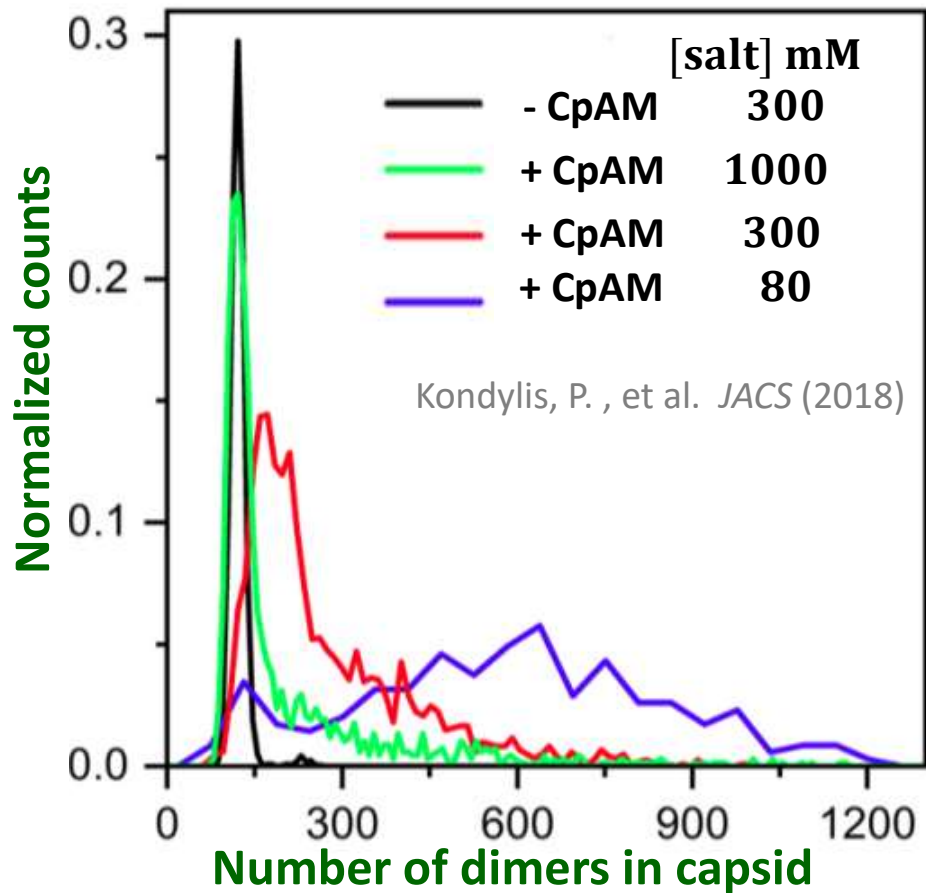


+ CpAM  
 $G_{\text{bind}} = 4.5 k_B T$

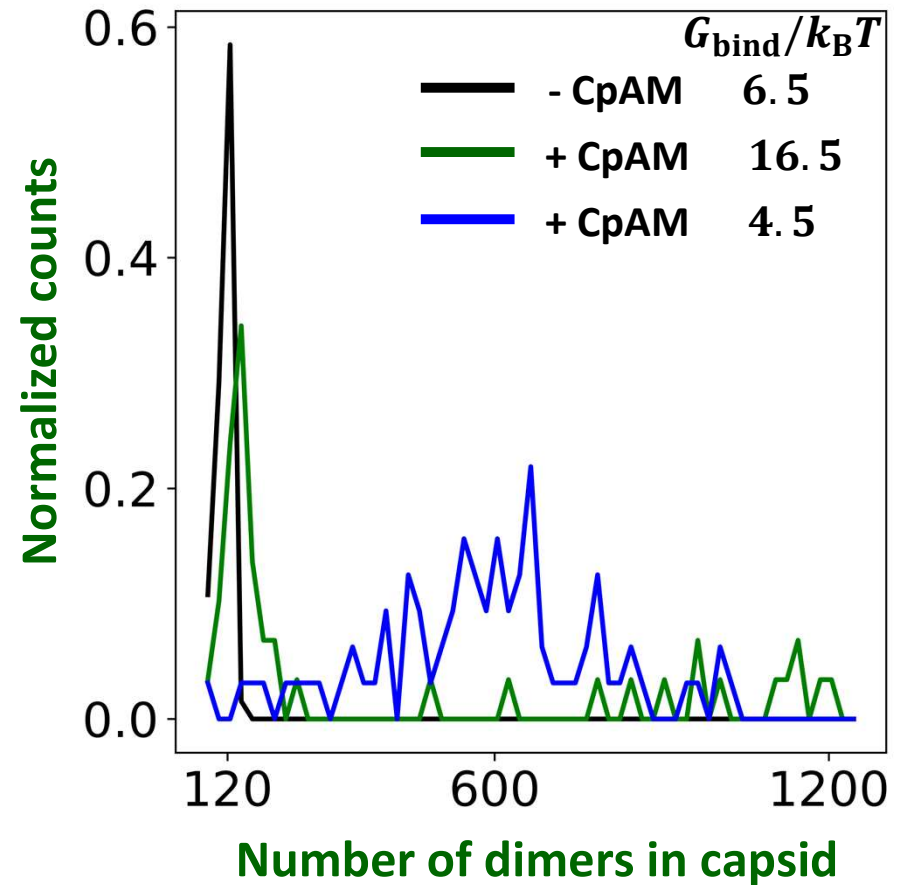


# Distribution of capsid sizes

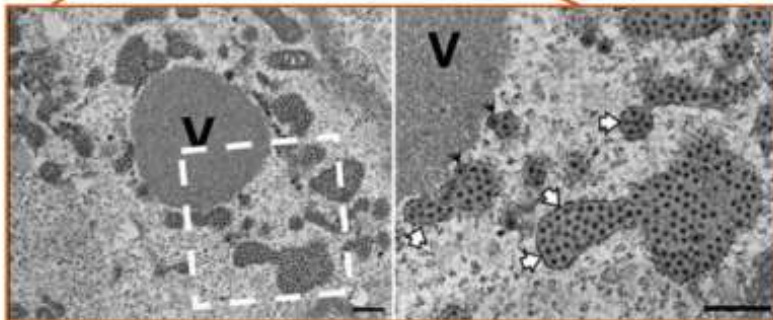
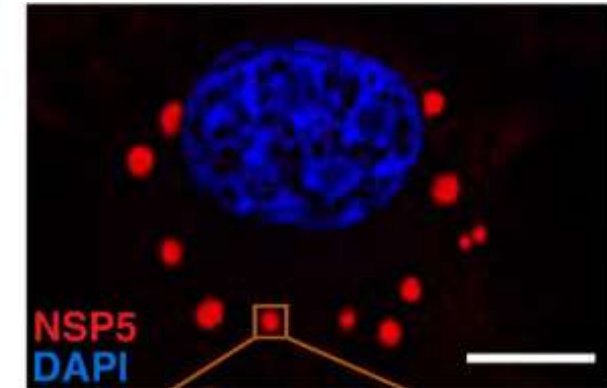
## Experiments



## Simulations



# Viruses exploit liquid-liquid phase separation (LLPS)



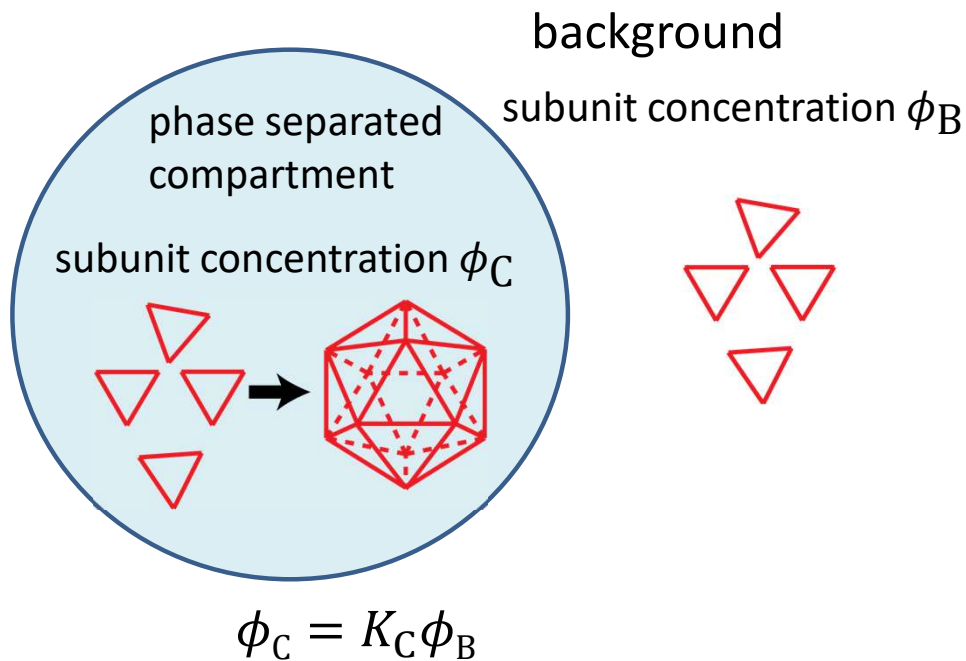
Cells infected by rotaviruses form phase separated compartments called viroplasm (V) within which new viral particles assemble

## Viroplasm: Assembly and Functions of Rotavirus Replication Factories

[Guido Papa](#)<sup>1</sup>, [Alexander Borodavka](#)<sup>2</sup>, [Ulrich Desselberger](#)<sup>3</sup>  
[Viruses](#). 2021 Jul; 13(7): 1349.  
doi: [10.3390/v13071349](https://doi.org/10.3390/v13071349)

See also: [Etibor et al.](#), *Viruses* 2021, 13, 366

# Self-Assembly Coupled to Liquid-Liquid Phase Separation (LLPS)

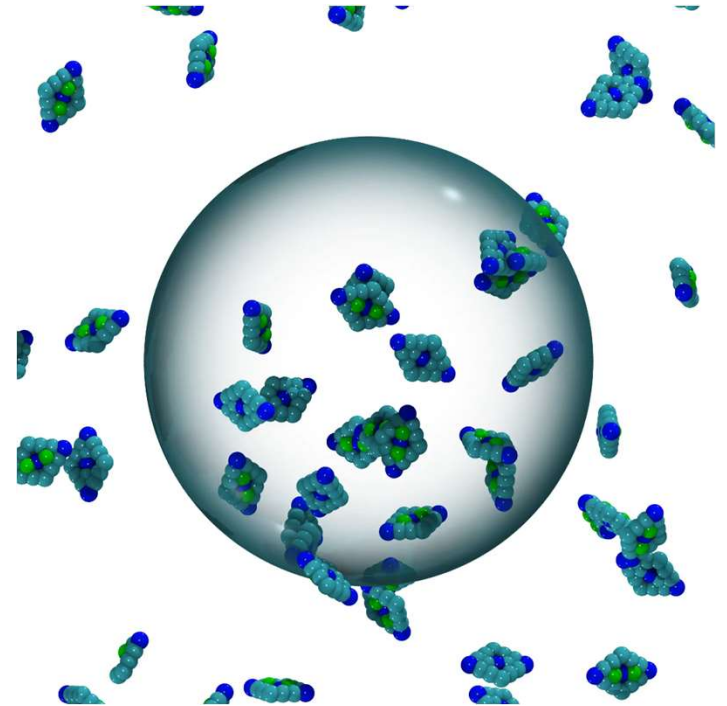
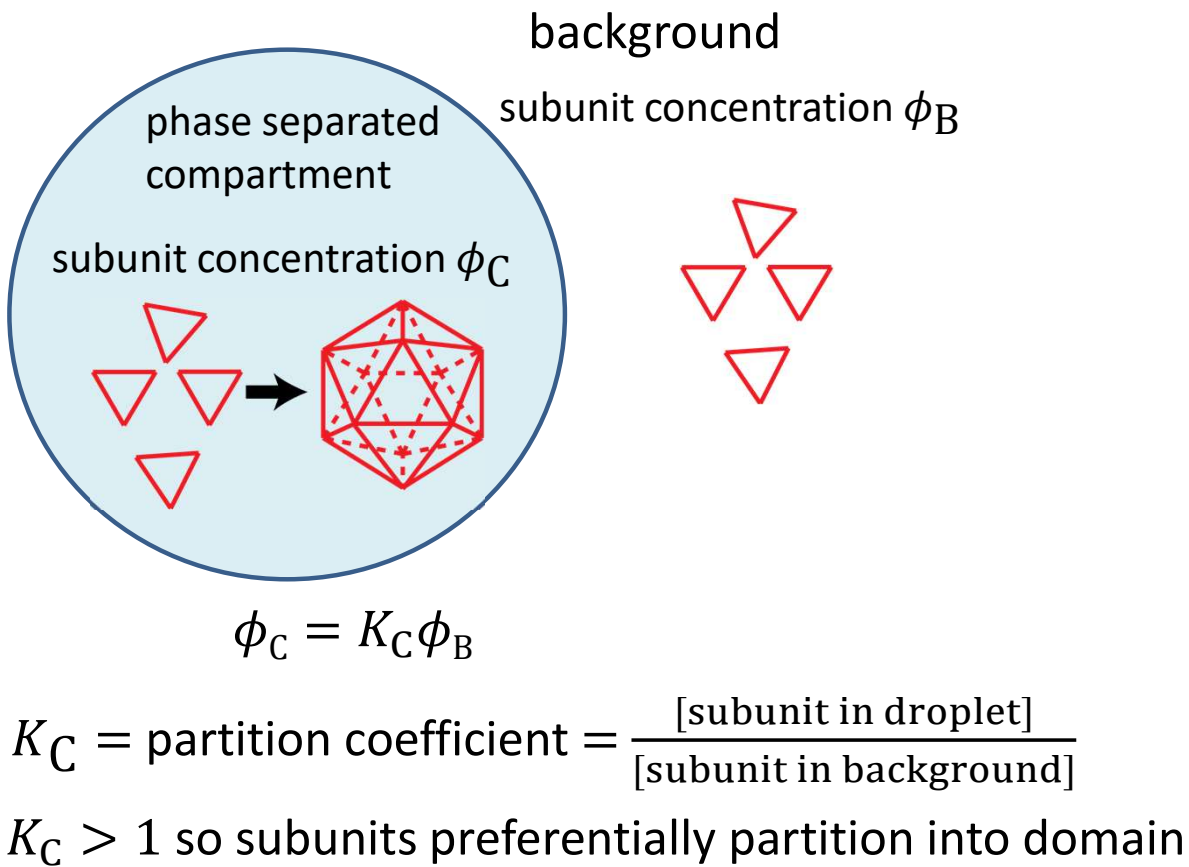


$$K_C = \text{partition coefficient} = \frac{[\text{subunit in droplet}]}{[\text{subunit in background}]}$$

$K_C > 1$  so subunits preferentially partition into domain

Hagan & Mohajerani, Plos Comp. Biol. (2023) <https://doi.org/10.1371/journal.pcbi.1010652>  
see also, Weber et al. eLife 2019;8:e42315 for similar model for irreversible filament assembly

# Self-Assembly Coupled to Liquid-Liquid Phase Separation (LLPS)



Naren  
Sundararajan

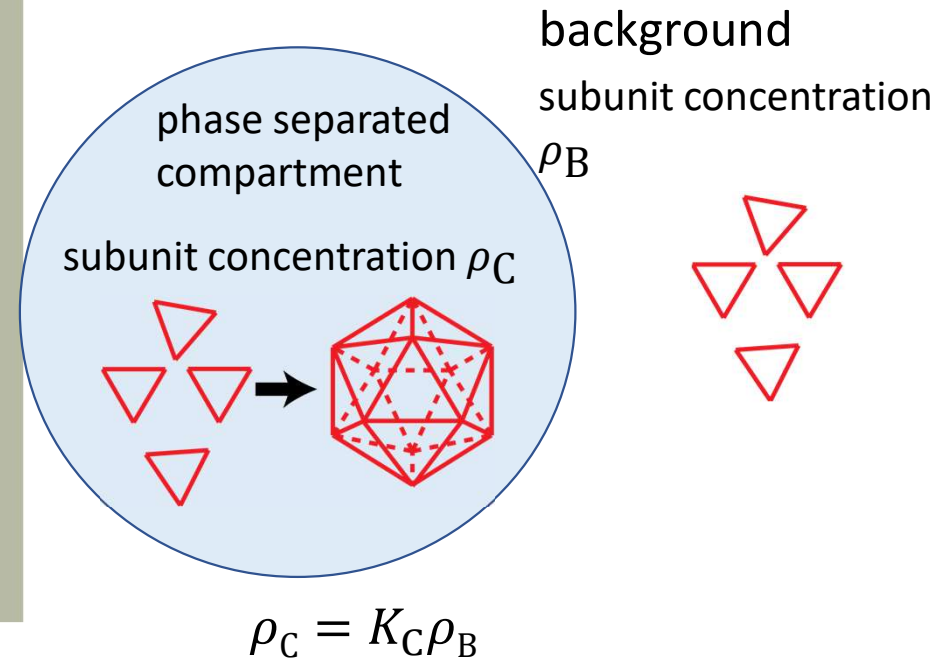


# Rate equation model for assembly coupled to LLPS

$$\frac{d\rho_1^\alpha}{dt} = -2f_1(\rho_1^\alpha)^2 + b_2\rho_2^\alpha + \left( \sum_{n=2}^{N-1} -f_n\rho_n^\alpha\rho_1^\alpha + b_n\rho_n^\alpha \right) + b_N\rho_N^\alpha + \mathcal{D}_1^\alpha$$

$$\frac{d\rho_n^\alpha}{dt} = f_{n-1}\rho_1^\alpha\rho_{n-1}^\alpha - (f_n\rho_1^\alpha + b_n)\rho_n^\alpha + b_{n+1}\rho_{n+1}^\alpha + \mathcal{D}_n^\alpha \quad \text{for } n = 2 \dots N-1$$

$$\frac{d\rho_N^\alpha}{dt} = f_{N-1}\rho_1^\alpha\rho_{N-1}^\alpha - b_N\rho_N^\alpha + \mathcal{D}_N^\alpha$$

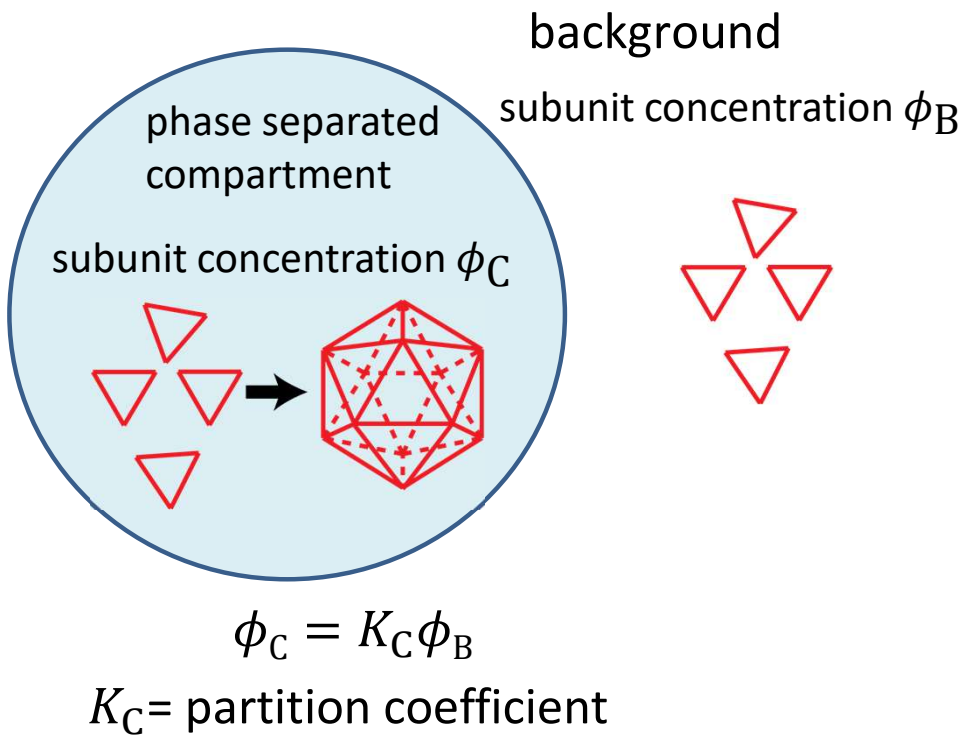


$$\mathcal{D}_n^c = \frac{1}{V_c} k_{DL}(n) (\rho_n^{bg} - \rho_n^c / K_c^n)$$

$$\mathcal{D}_n^{bg} = -V_r \mathcal{D}_n^c$$

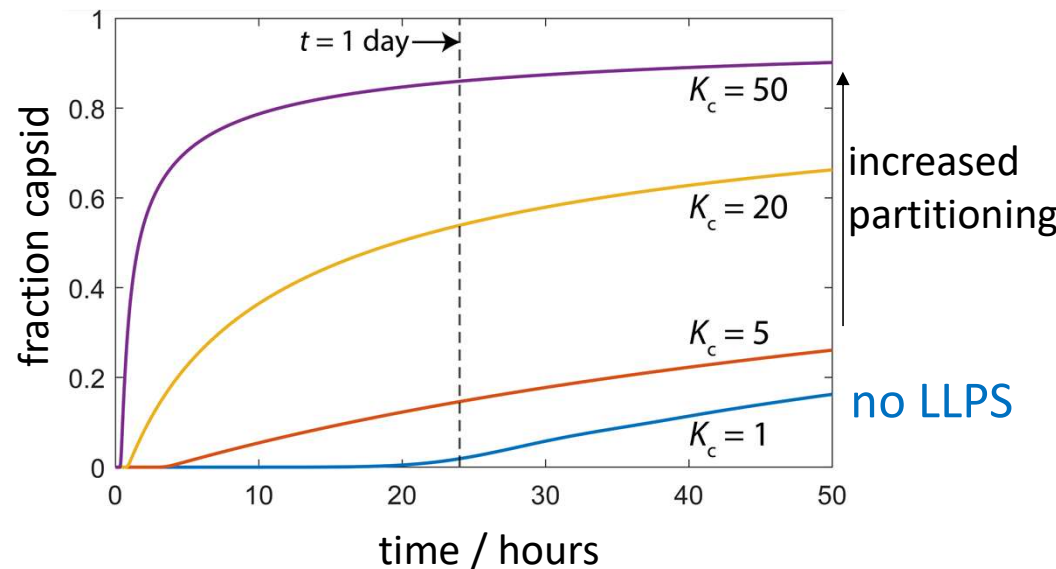
Hagan & Mohajerani, Plos Comp. Biol. (2023)

# Self-Assembly Coupled to Liquid-Liquid Phase Separation (LLPS)



$K_C > 1$  so subunits preferentially partition into domain

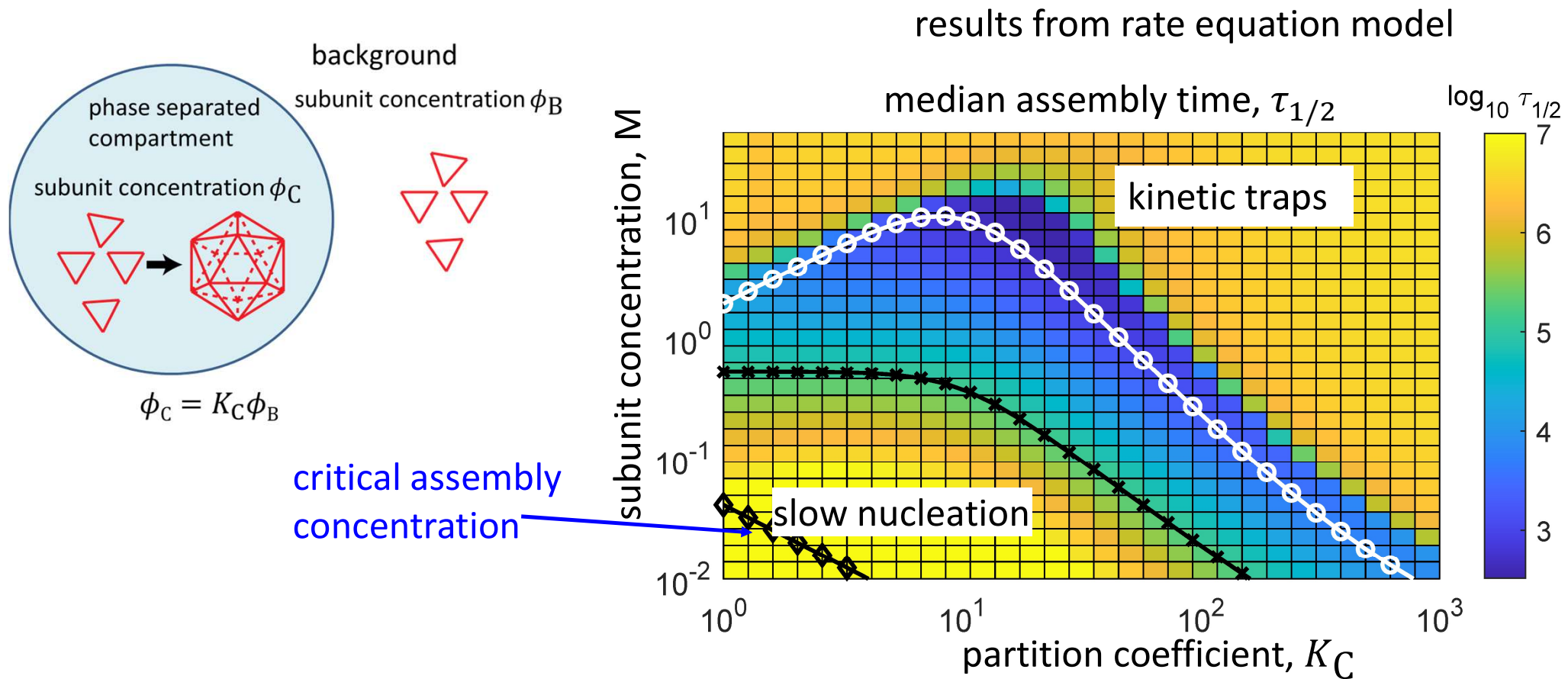
results from rate equation model



LLPS can increase assembly rates by orders of magnitudes



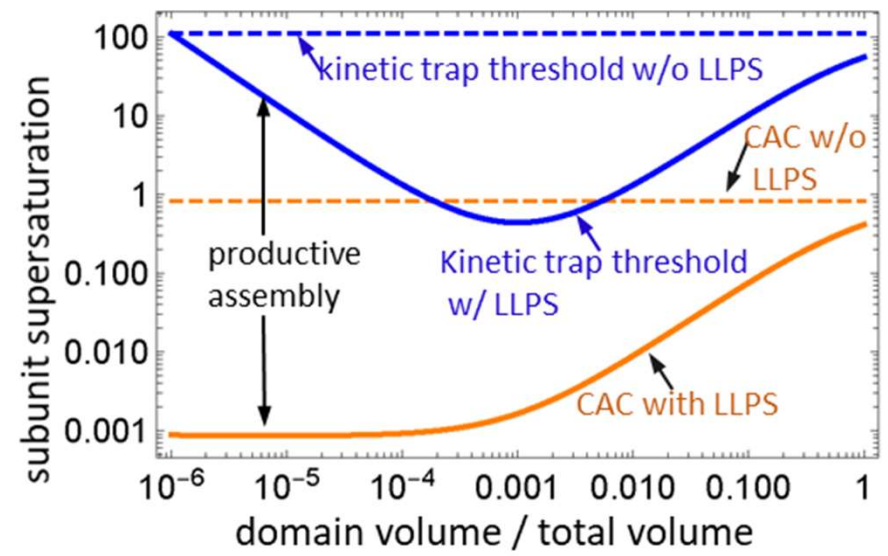
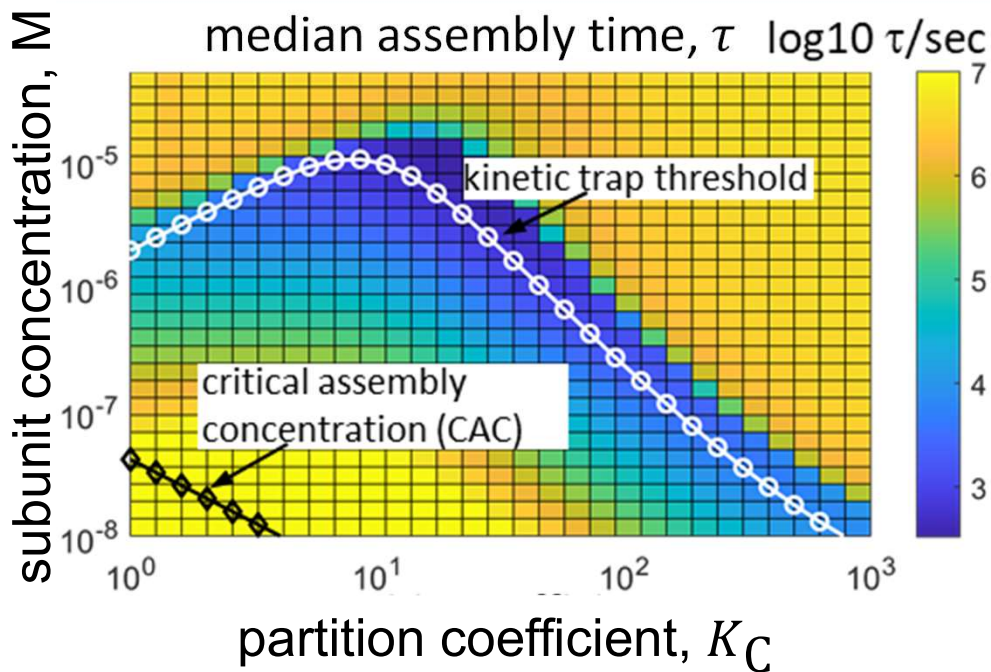
# Self-Assembly Coupled to Liquid-Liquid Phase Separation (LLPS)



LLPS increases assembly rates and **robustness to parameter variation**

Hagan & Mohajerani, Plos Comp. Biol. (2023) <https://doi.org/10.1371/journal.pcbi.1010652>

# Self-Assembly Coupled to Liquid-Liquid Phase Separation



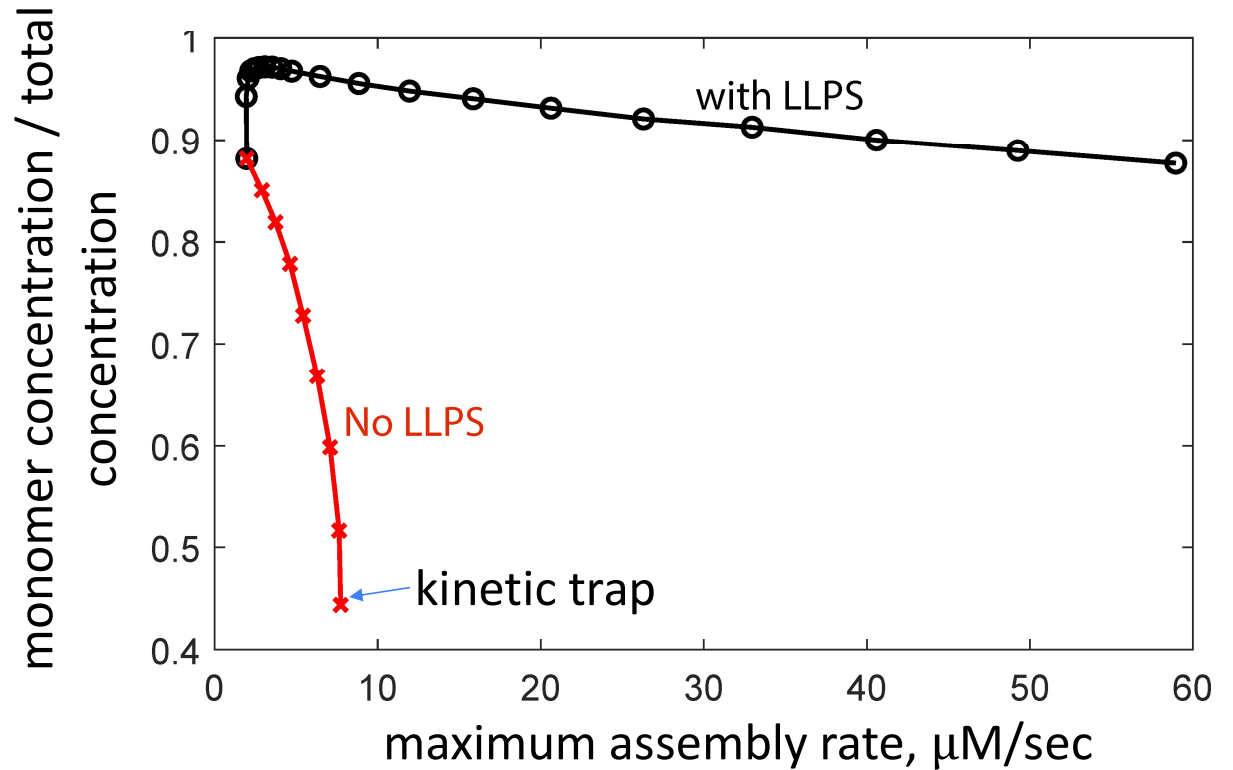
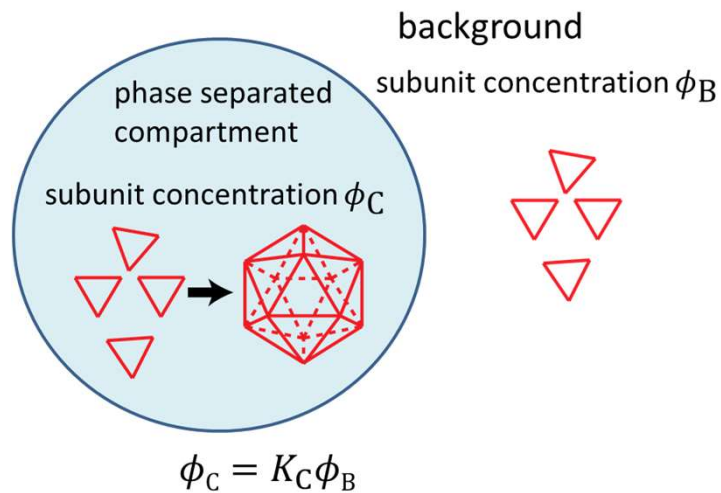
LLPS can:

- dramatically accelerate assembly rates
- make assembly robust, by expanding range of concentrations and binding affinities that lead to good assembly, by avoiding kinetic traps

$$\text{partition coefficient} = K_C = \frac{[\text{subunit in droplet}]}{[\text{subunit in background}]}$$

Hagan & Mohajerani, Plos Comp. Biol. (2023) <https://doi.org/10.1371/journal.pcbi.1010652>  
 see also, Weber et al. eLife 2019;8:e42315 for similar model for irreversible filament assembly

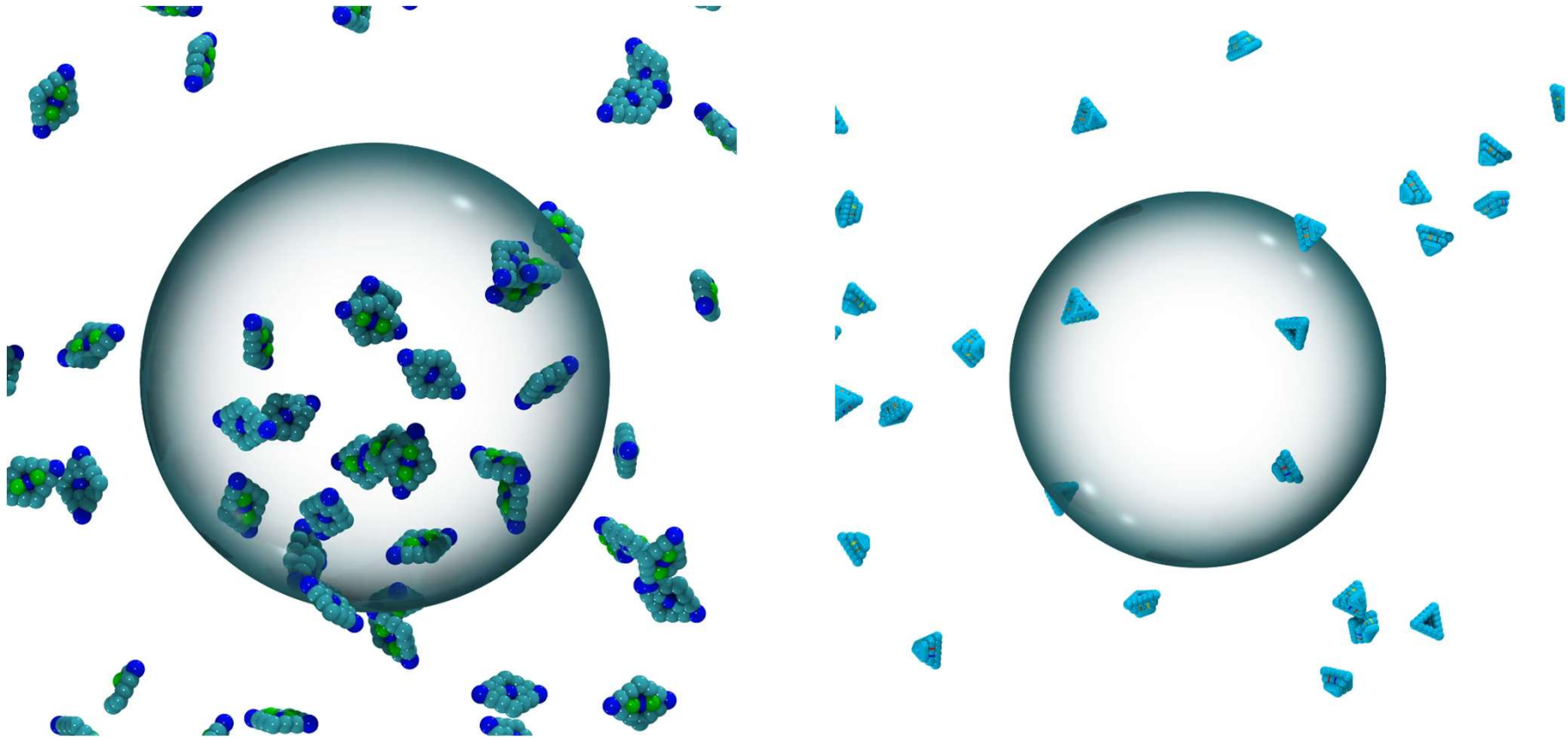
# Bulk solution acts as a buffer of free subunits



increasing concentration or interaction strength

fast assembly without depleting subunits because assembly is localized to compartment

# Brownian dynamics simulation of self-assembly with LLPS



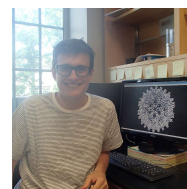
Naren  
Sundararajan



Farri  
Mohajerani



Naren  
Sundararajan



Chris  
Schlicksup



Adam  
Zlotnick



Jodi  
Hadden-Perilla

Botond Tyukodi, Stefan Paquay, Seth Fraden, Ben Rogers, Wei-Shao Wei

**NIH (R01GM108021)**

\$\$: DOE: Machine learning approaches to understanding  
and controlling 3D active matter

NSF (CMMT DMR-1855914, **Brandeis MRSEC**)

Brandeis Provosts Research Grant

Computation: NSF XSEDE, Brandeis HPCC

Hagan Group: Layne Frechette, Fernando Caballero,  
Anthony Trubiano, Phu Tran, Chris Amey, Yingyou Ma,  
Saptorshi Ghosh, Sarvesh Uplap, Naren Sundararajan,  
Smriti Pradhan



Postdoc position on active matter available

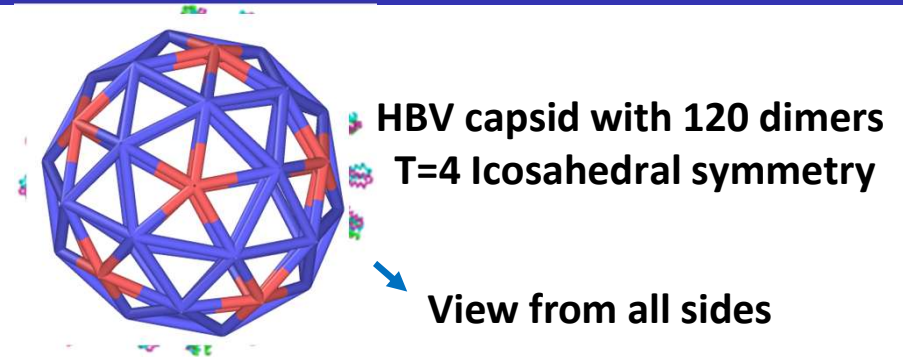
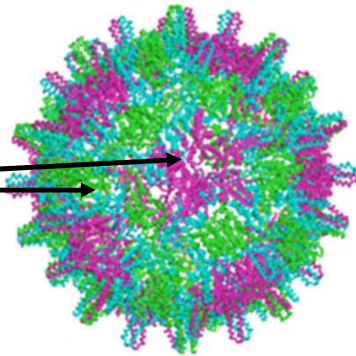
Brandeis MRSEC, AMC Crawford Notch, New Hampshire, 2023

# Capsid symmetry

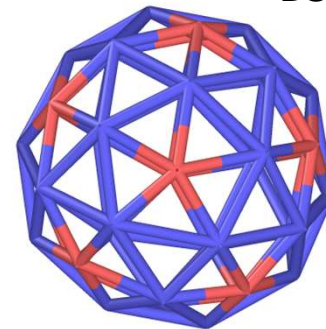
Model capsids with 120 dimers do not have icosahedral symmetry

preliminary results: 2 dimer conformations are required for T=4 symmetry

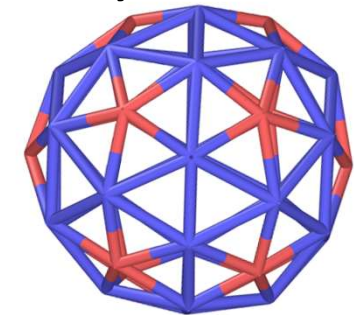
2 dimer conformations in T=4 HBV capsids



Model capsid with 120 edges  
D5h symmetry



Top view



Side view

Other works showing D5h is favored: Wagner & Zandi, Biophys. J. (2015); Sanaz, Li, Zandi 2018; Lorente, Hernandez-Rojas, Breton, Soft Matter (2018)