A review of progress on the design and analysis of adaptive parallel solvers for PDEs on surfaces will be presented. Domain decomposition solution paradigms which include monolithic or alternating mesh and physical PDE solves will be reviewed along with a summary of theoretical results. Recently developed solvers and preconditioners which utilize an embedding closest point method and a PETSc based implementation will be presented.