Over a local and over a global field, we consider complete intersections of two quadrics in n-dimensional projectif space, with n =4,5,6,7.

We discuss existence of lines and conics defined over the ground field and give some applications to the Hasse principle for rational points over a global field.