

Title: Polynomials corresponding to maximal rings and the Bertini theorem for $P^1(\mathbb{Z})$

Abstract: Let $n > 2$ be a fixed integer. Lenstra conjectured that when monic integer polynomials of degree n are ordered by the size of their largest coefficient, the proportion of polynomials which correspond to maximal rings is $1/\zeta(2)$, independent of n . In this talk, we will discuss the analogous question for the space of all (not necessarily monic) integer polynomials of degree n , and prove that a proportion of $1/(\zeta(2)\zeta(3))$ of them correspond to maximal rings, obtaining also the Bertini (regularity) theorem for $P^1(\mathbb{Z})$. This is joint work with Manjul Bhargava and Xiaoheng Wang.