Title: A stochastic maximal function and regularity estimates for parabolic stochastic evolution equations.

Abstract: We introduce a stochastic maximal funtion to facilitate regularity estimates for parabolic evolution equations given in terms of a analytic generator on a UMD Banach space (which include L-p spaces with 1<p<00 and their subspaces) and a cylindrical Brownian motion.