In joint work with Olga Kharlampovich, we show that finitely generated free groups of rank at least 3 lack a model-theoretic property called universal homogeneity. We also show that countable groups that are elementarily equivalent to non-abelian free groups, with the extra condition that any finitely generated abelian subgroups are cyclic, are unions of chains of hyperbolic towers.